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RuAl₆—An Endohedral Aluminide Superconductor

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ABSTRACT: Superconductivity is reported in an endohedral aluminide compound, RuAl₆, with $T_c = 1.21$ K. The normalized heat capacity jump at $T_c \Delta C/\gamma T_c = 1.58$, confirms bulk superconductivity. The Ginzburg–Landau parameter of $\kappa = 9.5$ shows that RuAl₆ is a type-II superconductor. Electronic structure calculations for RuAl₆ are explored in comparison to its structural analogue ReAl₆ ($T_c = 0.74$ K). The stability of the phases is discussed in terms of the crystal orbital Hamilton population (–COHP) analysis. The difference in T_c in the two materials is caused by the significantly stronger electron–phonon coupling found in RuAl₆, which is a result of significantly stronger antibonding interactions. The presence of



superconductivity in yet another compound made of aluminum clusters possibly expands the correlation of critical temperature and the structure shown for Ga-built clusters.

INTRODUCTION

One of the still unresolved problems of solid-state sciences is the design principle for superconductors, especially with high critical temperatures. The great effort to find universal relations that can be exploited to truly design superconducting materials led to a number of mostly empirical guidelines, such as the famous, semianecdotal Matthias rules.¹ Empirical relations between the superconducting critical temperature (T_c) and electron count per atom were also established in several groups of superconductors, including simple metallic elements,² A-15 compounds,³ as well as Heusler⁴ and high-entropy alloys.⁵

Recently, a group of gallium-rich intermetallic compounds, ReGa₅, Rh₂Ga₉, and Mo₈Ga₄₁, whose crystal structures are composed of interconnected endohedral Ga clusters, was found to be a host system for superconductivity with observed strong correlations between electron count, crystal structure, and superconducting critical temperature.⁶ In this broad family of compounds, the crystal and electronic structures can be described by considering the whole basic cluster, instead of single atoms, as the main building block.⁶

Interestingly, while Rh₂Ga₉ and Ir₂Ga₉ are superconductors with $T_c = 1.9$ and 2.2 K, respectively,⁷ the isoelectronic aluminides T_2 Al₉ (T =Co, Rh, Ir) do not show superconductivity down to T = 2 K (see ref 8 and Figure S6 in the Supporting Information (SI)). It is also worth noting that a subtle difference between the crystal structures of T_2 Ga₉ and T_2 Al₉ phases exists, the former crystallizing in a noncentrosymmetric structure variant.^{7,9} Aluminide analogues of the ReGa₅ and Mo₈Ga₄₁ intermetallics are not known.

In this study, we report superconductivity in RuAl₆ with $T_c = 1.21$ K. The crystal structure of RuAl₆ (Figure 1), reported previously in 1968 by Edshammar,¹⁰ can be described as a network of RuAl₁₀ polyhedra sharing edges along the *c* direction and corners along the *a* and *b* directions.



Figure 1. (a) Unit cell of RuAl_6 : Ru atoms are shown in brown, Al in blue. RuAl_{10} clusters share edges along the *c* direction and corners along the *a* and *b* directions. (b) RuAl_{10} cluster with the three individual Al sites labeled.

The observation of the superconducting state in RuAl_6 supports the hypothesis of a high prevalence of superconductivity in the class of endohedral intermetallics. Along with the recently reported isostructural compound ReAl₆ ($T_c = 0.74 \text{ K}$),^{11,12} RuAl₆ forms one of the branches of the endohedral superconductor family.

Moreover, we observe a relationship between T_c and nearest-neighbor (NN) antibonding interactions in ReAl₆ and RuAl₆ and postulate that it is caused by their effects on the phonon structure, which in turn affects the electron–phonon coupling (EPC). We highlight that the relation between antibonding population (measured using the crystal orbital overlap population function, COHP) and super-

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conductivity may be used as a simple guide for predicting superconductivity in new compounds.

MATERIALS AND METHODS

Polycrystalline samples of RuAl₆ were synthesized via an arc-melting method. Ru (Alfa Aesar, 99.95%) and Al pieces (Alfa Aesar, 99.99%) were put together on a water-cooled copper hearth with a Zr button used as an oxygen getter. The sample was turned and remelted several times to ensure homogeneity. Mass loss during synthesis was lower than 1%. The sample was then wrapped in thin tantalum foil, put in an evacuated quartz tube, and annealed at T = 620 °C (~40 °C below the melting point of Al and Al-rich eutectic¹³) for 14 days. After annealing, the ampoule was quenched in water at room temperature.

The powder X-ray diffraction (PXRD) pattern was collected at room temperature on a crushed sample with a Bruker D8 Focus diffractometer with Cu K α radiation. FullProf software¹⁴ was used for the Rietveld refinement of the RuAl₆ structure. The PXRD pattern of the annealed sample showed that a RuAl₆ phase was obtained with no observable amounts of impurity phases.

Single crystals of RuAl₆ were grown using a self-flux method.^{15,16} Ru and Al pieces in a molar ratio of 3:97 were put in an alumina crucible, sealed in an evacuated quartz tube, heated to 1000 °C, slowly cooled to 670 °C, and subsequently centrifuged to remove the remaining Al flux. However, they were found to be contaminated with Al metal. Centrifugation above the melting point of Al (3000 rpm) and prolonged etching in a sodium hydroxide solution did not remove all of the elemental Al, which may be present in the form of inclusions within the crystals, as it was observed, e.g., in Al flux-grown SmB₆,¹⁷ bulk Al shows a transition to the superconducting state at $T_c = 1.2$ K, overlapping with the T_c of RuAl₆. To avoid ambiguity, physical property measurements were performed only on a polycrystalline sample that was proven to be free of impurity phases, including Al (see Figures 2 and S2 in the Supporting Information).

Magnetization measurements were performed with a Quantum Design MPMS-XL SQUID magnetometer in a temperature range of T = 0.5-2.5 K and in a magnetic field of up to $\mu_0 H = 100$ mT. Electrical resistivity was measured using a standard four-probe technique¹⁸ with a Quantum Design Physical Property Measurement System (QD PPMS) in a temperature range of T = 0.4-300 K and in a magnetic



Figure 2. Rietveld fit (black line) to the room-temperature PXRD pattern (red dots) of $RuAl_6$. The blue line shows the difference between calculated and observed intensities. The green color marks the expected positions of Bragg reflections.

field of up to $\mu_0 H$ = 350 mT, with temperatures T < 1.9 K reached using a ³He evaporative cooling option.¹⁹ A silver epoxy paste was used to attach platinum electrical contacts to the sample. Heat

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used to attach platinum electrical contacts to the sample. Heat capacity measurements employing the standard semiadiabatic pulse technique^{20,21} were done in the temperature range of 0.2-3 K using the ³He⁻⁴He dilution refrigerator option of the QD PPMS.^{22–24}

To gain insight into the chemical bonding in RuAl₆ and the analogous ReAl₆ compound, calculations of the crystal orbital Hamilton population (–COHP)^{25,26} were performed within the density functional theory (DFT) tight-binding linearized muffin-tin orbital atomic sphere approximation (TB–LMTO–ASA) as implemented in the Stuttgart code^{27,28} employing the Perdew–Wang generalized gradient approximation (GGA) for the exchange-correlation potential.²⁹ Calculations were conducted using a 16 × 16 × 8 *k*-point mesh and experimental unit cells.

Detailed band structure and electronic density of states (DOS) calculations were performed by means of the DFT with the Perdew–Burke–Ernzerhof³⁰ GGA utilizing the ELK all-electron full-potential linearized augmented plane wave plus local orbitals code.³¹ Calculations were conducted with spin–orbit coupling (SOC) using an $8 \times 10 \times 7$ k-mesh.

RESULTS AND DISCUSSION

The room-temperature powder X-ray diffraction pattern is presented in Figure 2. All of the Bragg peaks in the PXRD pattern are indexed with an orthorhombic *Cmcm* unit cell.

The lattice parameters and atomic positions obtained from the fit are in good agreement with those reported in the literature.¹⁰ Table 1 presents the details of the $RuAl_6$ crystal structure derived from the Rietveld refinement.

Table 1.	Crystal	lographic l	Data	for RuA	1 ₆ 0	btained	from	the
Rietveld	Fit to	the PXRD	Patte	ern ^a				

	Cmcm (# 63)			
Pearson symb	ol			oS28
unit cell parar	neters (Å)			
<i>a</i> =				7.48502(1)
<i>b</i> =				6.55652(1)
<i>c</i> =				8.97105(1)
cell volume (A	Å ³)			440.402(1)
molar weight	262.96			
number of for	4			
density (calcu	3.97			
figures of mer	it			
$R_{\rm p}$ (%)				12.1
R_{wp} (%)				9.81
$R_{\rm exp}$ (%)				6.77
χ^2				2.10
atom	x	у	z	B (Å ²)
Al(1)	0.3196(1)	0	0	1.11(2)
Al(2)	0	0.1412(1)	0.1000(1)	1.62(2)
Al(3)	0.3207(1)	0.2942(1)	1/4	1.02(2)
Ru	0	0.4620(1)	1/4	0.44(1)

^{*a*}Numbers given in parentheses are statistical uncertainties of the least significant digits. The *R* factors given are the conventional Rietveld *R* factors (background-corrected) calculated only for points with Bragg contributions.^{32,33}

The zero-field-cooled (ZFC) and field-cooled (FC) dc magnetic susceptibilities are shown in Figure 3a. The onset of the transition to the superconducting state is visible in both ZFC and FC plots at $T_c = 1.25$ K. This temperature is defined as the temperature where the extrapolation of the steepest slope of $\chi(T)$ intersects the extrapolation of the normal state



Figure 3. (a) Temperature-dependent ZFC and FC magnetization at an applied field of $\mu_0 H = 2.5$ mT, showing the transition to a perfectly diamagnetic Meissner state below T = 1.25 K. The volume susceptibility χ_V is corrected for the demagnetization factor derived from M_V vs H measurement (see (b,c)). Field-dependent magnetization below the T_c (inset to (a)) shows that RuAl₆ is a type-II superconductor. (b) Field-dependent magnetization curves measured at different temperatures below T_c . The black solid line is a linear fit in the low field limit. (c) Method of estimating the lower critical field, H_{c1} . (d) Lower critical field $H_{c1}^*(0)$ estimation.

susceptibility to lower temperatures.³⁴ After correction for the diamagnetic factor (discussed below), the magnitude of the saturated ZFC diamagnetic signal is close to the value of $-1/4\pi(1 - N)$ consistent with a full Meissner state (perfect diamagnetism), indicative of a complete transition to the superconducting state. The much smaller FC diamagnetic signal originates from the strong magnetic flux pinning present in the polycrystalline sample.

The volume magnetization vs magnetic field $M_v(H)$ plot measured at various temperatures below T_c is shown in the inset of Figure 3b. Assuming that a perfect diamagnet has a linear response to the magnetic field, the M_v vs H plot constructed at the lowest temperature (0.5 K) was fitted with a linear function $(M_{fit} = aH + b)$. The value of the demagnetization factor (N) is then estimated using the equation $-a = \frac{1}{4\pi(1-N)}$ and is equal to N = 0.33. The demagnetization factor accounts for a sample shape-dependent distortion of the magnetic field inside and around a sample.³⁵ To plot the $(M_v - M_{fit})$ vs H graph in Figure 3c, the linear fit to the initial magnetization slope was constructed. The fields in which deviations from a linear response to the magnetic field are visible (marked with the black dashed line in Figure 3c) were taken as lower critical fields H_{c1}^* . The H_{c1}^* values derived for different temperatures were plotted vs temperature in Figure 3d and fitted with the equation $\mu_0 H_{c1}^*(T) =$ $\mu_0 H_{c1}^*(0) [1 - (T/T_c)^2]^{.36}$ The value of critical field extrapolated to T = 0 K using the fitted function is $\mu_0 H_{c1}^*(0) = 3.60(7)$ mT. This value has to be corrected for the demagnetization factor, yielding $\mu_0 H_{c1}(0) = 5.4(1)$ mT. The critical temperature estimated from the fitting of the model to the data $T_c = 1.21(1)$ K is close to the value obtained from dc magnetization measurement. The full magnetization loop collected at a temperature of T = 0.5 K, below the

superconducting transition, is shown in the inset of Figure 3a. The shape of the M(H) loop suggests that $RuAl_6$ is a type-II superconductor.^{36,37}

To further characterize the superconducting transition of RuAl₆, electrical resistivity measurements were performed in the temperature range of T = 0.4-300 K, presented in Figure 4a. At temperatures above T_{c} , RuAl₆ shows typical metallic



Figure 4. (a) Electrical resistivity of RuAl_6 at zero applied magnetic field, showing typical metallic behavior at high temperatures and a drop to zero below T_{ci} the inset shows the SC transition being suppressed by the applied magnetic field. (b) Dependence of the upper critical field H_{c2} on temperature. (c) Pronounced heat capacity anomaly at T_{ci} confirming the bulk nature of the SC transition; the electronic heat capacity coefficient γ and Debye temperature are shown.

behavior, with a residual resistivity ratio RRR = $\rho_{300}/\rho_0 \approx 4$, falling in the range typical for polycrystalline samples, ^{4,38,39} and residual resistivity $\rho_0 = 0.038 \text{ m}\Omega \text{ cm}$.

The inset of Figure 4a presents the shift of superconducting transition toward lower temperatures with an applied magnetic field. The midpoints of the transitions gathered in this measurement were used to determine the upper critical shown in Figure 4b. The data were fitted with the formula proposed by Micnas et al.:⁴⁰ $\mu_0 H_{c2}$ (T) = $\mu_0 H_{c2}$ (0)[1 – (T/T_c)^{3/2}]^{3/2} and gave the value $\mu_0 H_{c2}(0)$ = 426(7) mT, which will be used in further calculations.

Using the value of $\mu_0 H_{c2}(0)$ obtained from the fit and assuming that H_{c2} is purely due to orbital effects, the coherence length ξ_{GL} can be estimated from the equation $H_{c2}(0) = \phi_0/2\pi\xi_{GL}^2$ (where $\phi_0 = h/2e$ is the quantum of magnetic flux)^{41,42} and is equal to $\xi_{GL} = 27.7(2)$ nm.

Heat capacity measurements on a RuAl₆ sample were performed to confirm the bulk nature of its superconductivity. Figure 4c shows the transition to the superconducting state of RuAl₆ without the applied magnetic field. A sharp anomaly confirms the bulk superconductivity. An equal-area entropy construction (solid black lines) was used to extract the transition temperature and the value of the specific heat jump. The superconducting critical temperature was determined to be $T_c = 1.21$ K, and the specific heat jump is $\Delta C_p/T = 10.3$ mJ mol⁻¹ K⁻². Figure 4d shows the heat capacity of RuAl₆ as the C_p/T vs T^2 plot, fitted above the T_c using the formula of the low-temperature expansion of the Debye heat capacity model: $C_p/T = \gamma + \beta T^2$, where γT and βT^3 are the electronic and phonon heat capacity contributions, respectively.⁴² The fit yields $\gamma = 6.5(1) \text{ mJ mol}^{-1} \text{ K}^{-2}$ and $\beta = 0.14(1) \text{ mJ mol}^{-1} \text{ K}^{-4}$. The Debye temperature is then calculated using β via the relation

$$\Theta_{\rm D} = \sqrt[3]{\frac{12\pi^4 nR}{5\beta}}$$

where *n* is the number of atoms per formula unit (n = 7) and *R* is the gas constant. The resulting Debye temperature is $\Theta_D = 458(12)$ K. Taking the obtained γ , the normalized jump in specific heat equals $\Delta C/\gamma T_c = 1.58$, which is above the lower limit (1.43) predicted for weak coupling superconductors by the BCS theory, suggesting a bulk transition to the superconducting state.

To exclude the possibility that the superconducting transition is caused by an elemental Al impurity ($T_c = 1.2$ K), the heat capacity sample was ground after the measurement and a PXRD pattern was collected. The results (Figure S2 in the Supporting Information) show no observable amount of Al, confirming the bulk superconductivity of RuAl₆.

An alternative way of estimating the upper critical field of B C S superconductor is via the relation $H_c(0) = -AT_c \frac{dH_c}{dT}\Big|_{T=T_c}$, where A is a coefficient taking the value of 0.69 or 0.73 for the dirty or clean limit, respectively.⁴³ Taking $T_c = 1.21$ K and the slope of the $\mu_0 H_{c2}(T)$ data (Figure 4b) $d\mu_0 H_{c2}/dT = -0.426$ T/K, the calculation gives values of $\mu_0 H_{c2} = 360$ and 380 mT for the dirty and clean limits, respectively.

The superconducting London penetration depth $\lambda_{\rm GL}$ can be estimated from the formula $H_{\rm c1} = \frac{\phi_0}{4\pi\lambda_{\rm GL}^2} \ln \frac{\lambda_{\rm GL}}{\xi_{\rm GL}}$. The estimated value of penetration depth for RuAl₆ is $\lambda_{\rm GL} = 265$ nm. The Ginzburg–Landau parameter is calculated as $\kappa = \lambda_{\rm GL}(0)/\xi_{\rm GL}(0) = 9.5$. This value is significantly higher than $1/\sqrt{2}$, and the Ginzburg–Landau theory classifies RuAl₆ as a type-II superconductor, in contrast to type-I ReAl₆. The upper and lower critical fields can be linked to the thermodynamic critical field via the Ginzburg–Landau parameter: $H_{\rm c1}H_{\rm c2} = H_{\rm c2} \ln \kappa^{44}$ and gives the value of $\mu_0 H_{\rm c} = 32$ mT.

All superconducting parameters are summarized in Table 2 and compared to results reported for ReAl₆ in ref 11.

The band structures and DOS of RuAl₆ and ReAl₆ are shown in Figure 5. DOS projections show that in both cases, the majority of $DOS(E_F)$ is contributed by Al s and p orbitals, with the majority of Ru/Re *d* contribution lying well below the E_F . As shown in Figure S4 in the Supporting Information, the effects of SOC on the band structure of RuAl₆ were found to be negligible, while for ReAl₆, only minor differences were found between results calculated with and without SOC within 1 eV from the Fermi level. This is consistent with the fact that DOS around E_F is mostly contributed by Al s and p states. Since SOC has only negligible effects on the electronic structure, calculations of COHP using the scalar-relativistic TB–LMTO–ASA code can be considered reliable.

Surprisingly, the DOS($E_{\rm F}$) of both compounds was found to be very similar (<3% difference) even though T_c differs by a factor of ~1.6 and the γ electronic heat capacity coefficient is 30–40% lower in ReAl₆ than in RuAl₆. The value of γ is proportional to DOS($E_{\rm F}$) but is also renormalized by electron–phonon interactions: $\gamma = \gamma_{\rm calc} (1 + \lambda_{\rm el-ph})$, where

Table 2. Summary of Normal and Superconducting State Parameters for RuAl₆ Compared to ReAl₆. Unless Marked with Asterisk, Values for the Latter are Taken from ref 11

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parameter	RuAl ₆	ReAl ₆
$T_{\rm c}$ (K)	1.21	0.74
$\mu_0 H_{c1}(0) \ (mT)$	5.4(1)	
$\mu_0 H_{c2}(0) \ (mT)$	426(7)	
$\mu_0 H_c(0) (mT)$	32	44-50
$\xi_{\rm GL} (\rm nm)$	27.7	
$\lambda_{\rm GL} \ ({\rm nm})$	265	
κ	9.5	
$\gamma (mJ mol^{-1} K^{-2})$	6.5(1)	3.9-4.7
$\Theta_{\rm D}$ (K)	458(12)	~400
$\Delta C_{ m el}/\gamma T_{ m c}$	1.58	1.37-1.42
$DOS(E_F)$ (states/eV/f.u.)	1.57	1.53*
$\gamma_{\rm calc} \ ({\rm mJ} \ {\rm mol}^{-1} \ {\rm K}^{-2})$	3.70	3.60*
$\lambda_{ m el-ph}$	0.81	0.08-0.31*



Figure 5. Band structure [(a), (c)] and density of states [(b), (d)] plots for RuAl₆ and ReAl₆ as obtained from the full-potential linearized augmented plane wave plus local orbital (FP-LAPW + LO) calculations. DOS in a wider energy range is shown in Figure S3 in the SI.

 $\gamma_{\rm calc} = \pi/3 \ k_{\rm B}^2 \cdot {\rm DOS}(E_{\rm F})$ is the value obtained from DOS calculations and $\lambda_{\rm el-ph}$ is the dimensionless EPC coefficient.

One can estimate the value of the EPC coefficient via the relation $\lambda_{\rm el-ph} = \frac{\gamma}{\gamma_{\rm calc}} - 1$. This yields $\lambda_{\rm el-ph} \approx 0.81$ for RuAl₆ and 0.08–0.31 for ReAl₆, suggesting that the difference in $T_{\rm c}$ in the two materials is caused by a significantly weaker EPC found in the latter.

In a simple form of the empirical McMillan formula,⁴⁵ T_c is linearly proportional to the Debye temperature

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$$T_{\rm c} = \frac{\Theta_{\rm D}}{1.45} \exp\left(\frac{-1.04(1+\lambda_{\rm el-ph})}{\lambda_{\rm el-ph} - (1+0.62\lambda_{\rm el-ph})\mu^*}\right)$$

where μ^* is the Coulomb pseudopotential parameter. Its value is equal to 0.1 in the case of nearly free electron metals and in cases the value of μ^* is assumed to be around 0.13; therefore, such a number is used for further estimations. The Θ_D value of RuAl₆ is only about 13% higher than that of ReAl₆ and cannot completely account for the increased T_c of the former. This suggests that the difference in T_c in the two materials is caused primarily by the difference in the EPC strengths, which in turn is affected strongly by the phonon spectrum.

The analysis of -COHP (Figure 6) shows that in RuAl₆, the peak in DOS near E_F derives from antibonding NN Ru–Al and



Figure 6. Crystal orbital Hamilton populations (-COHP) for $RuAl_6$ (a) and $ReAl_6$ (b) as obtained from TB-LMTO-ASA calculations.

Al–Al interactions (with the strongest contribution of Al_2-Al_2 in the latter case). The occupation of antibonding states is a driving force for instability toward either a crystal or electronic structure distortion. The latter may be manifested by an onset of itinerant ferromagnetism^{46–48} or superconductivity.^{49–53} In the case of RuAl₆, no structural transition is seen down to 2 K, as evidenced by heat capacity measurements (shown in Figure S1 in the Supporting Information) and thus, the electronic "strain" due to the antibonding electron population is reduced by opening a superconducting gap.

Out of all of the Al–Al pairs, the –COHP for Al₂–Al₂ shows the strongest antibonding interaction (Figure 6a). This results from the close contact between Al₂ atoms within the "void" and the RuAl₁₀ polyhedra seen in the [001] direction. Al₂ atoms form an infinite zigzag chain parallel to the *c* axis with alternating distances of $d_1 = 2.58$ and $d_2 = 2.69$ Å. Such apparently empty space is also seen in the PdGa₅-type structure, in which it was found to be a region of high electron density due to intracluster bonding.⁵⁴

Even though the unit cell parameters of RuAl₆ are smaller than those of ReAl₆, the Al₂-Al₂ distance is found to be shorter in the latter ($d_1 = 2.57$, $d_2 = 2.65$ Å). This highlights the effect of bond weakening by additional electrons occupying antibonding states.

In ReAl₆, the Re–Al states around $E_{\rm F}$ are of a bonding nature, but weak antibonding interactions between NN Al atoms are also observed. Since the DOS($E_{\rm F}$) of both compounds is almost the same, one can postulate that stronger antibonding interactions in RuAl₆ are, at least partially, responsible for the enhanced $T_{\rm c}$ through their influence on the EPC.

This suggests a way to further increase the T_c by electron doping RuAl₆ (partial Rh or Ir substitution for Ru)—while a small amount of dopant is expected to enhance T_c a larger pubs.acs.org/cm

amount will inevitably result in the destabilization of the crystal structure. This is in agreement with the fact that no MnAl₆-type phase is known to exist in the Rh–Al system, the most Alrich intermetal in the system being the endohedral cluster compound Rh₂Al₉.⁵⁵ COHP calculations for hypothetical "RhAl₆" show much stronger antibonding interactions (Figure 7a) and a DOS(*E*) peak (Figure 7b) near *E*_F, both in agreement with the instability of the structure.



Figure 7. (a) COHP curves for a hypothetical $RhAl_6$ compound compared to $RuAl_6$. (b) DOS for $RhAl_6$ calculated within the TB–LMTO–ASA approximation showing a DOS peak near E_F .

The presence of antibonding population results in a decrease in the bond strength and thus phonon mode softening. Allen and Cohen⁵⁶ discussed the positive correlation between mode softening and increased superconducting T_c in rocksalt-type transition-metal carbides, such as HfC ($T_c < 0.02$ K) and TaC ($T_c \approx 11$ K). In HfC, the Fermi level lies in the Hf–C bonding region (see Supporting Information Figure S4 for –COHP curves) and the additional electrons in TaC populate antibonding orbitals, leading to the decrease in the bonding strength. In our system, the effect on T_c is more subtle, yet it is still the likely reason for the enhanced transition temperature of RuAl₆ compared to ReAl₆

Figure 8 shows the MnAl₆-type crystal structure compared to other Al-rich binary phases of group 6–9 transition metals



Figure 8. Comparison of the crystal structures of Al-rich intermetallic compounds of group 6–9 transition metals (TMs).

(TMs). In each case, the total valence electron count (VEC) per TM atom is higher than 18, which suggests that significant direct Al–Al bonding is present.^{57–39} The decreasing coordination number of TM with increasing group number can be, at least partially, rationalized in terms of atomic contraction along the *d* series of the periodic table: a higher number of neighbors is expected around a larger atom. This phenomenon is also likely responsible for the lack of Ga

analogues of ReAl_6 and RuAl_6 as the atomic and covalent radii of Ga are larger than those of Al.^{60,61}

CONCLUSIONS

We have studied the superconductivity of RuAl₆. Resistivity, magnetic susceptibility, and heat capacity measurements show superconducting behavior with $T_c = 1.21$ K. RuAl₆ with 26 electrons per transition metal places itself on the rightmost part of the T_c vs e⁻ per transition metal diagram of endohedral superconductors.⁶ While there is recent evidence that the VEC- T_c behavior extends further to the low VEC region $(\text{Re}_8\text{Ga}_{19.8}\text{Zn}_{21.2} \text{ was reported to remain metallic at least down to } T = 1.8 \text{ K}^{62})$, the low-temperature (T < 2 K) physical properties of PdGa₅ (VEC = 25) and M_2Al_9 (M = Co, Rh, Ir) (VEC = 22.5) are not reported, and we cannot draw a conclusion whether RuAl₆ and, more generally, Al-based endohedral compounds family follow the trend observed for the gallide endohedral superconductors. An interesting question is whether the COHP analysis can explain the difference between isostructural V₈Ga₄₁ (no SC transition down to 2 K) and Mo₈Ga₄₁ ($T_c = 9.8$ K).⁶ Unfortunately, due to very large unit cells (48 atoms in the primitive cell), we were not able to perform such calculations. Further investigation of Al-built endohedral cluster superconductors is needed to fully outline the appearance of the diagram for T_c of such compounds.

Interestingly, according to the Topological Materials Database and Materiae, $^{63-67}$ RuAl₆ is a candidate topological material, making it a possibly useful system to study the interplay between superconductivity and topology.

Superconductivity is often observed at the edge of a structural transition, such as a charge density wave distortion. A classic example is elemental tellurium, which crystallizes in a trigonal α -Se structure, which can be derived from the simple cubic α -Po structure via a Peierls distortion.⁴⁷ The distortion can be rationalized in terms of reduction of strong antibonding interactions present in the case of Te in the α -Po-type structure.⁴⁷ If, however, the distortion is suppressed by the application of high pressure, Te becomes metallic and shows superconductivity with $T_c \approx 7.5$ K.⁶⁸ Note that while the high-pressure structure of Te is body-centered cubic instead of simple cubic, the strong antibonding Te—Te interactions are still present.⁶⁹

This competition between the structural distortion and superconductivity is observed in various other systems (e.g., TiSe_2^{70}) and in general can be seen as stemming from two competing phenomena induced by the strong EPC: T_c is enhanced by an increase of EPC, but only to the point where a strong EPC destabilizes the original structure, resulting in more strongly bonded one with lower $\text{DOS}(E_{\rm F})$ and suppressed T_c .

The correlation between T_c and the antibonding population, as observed in RuAl₆ and ReAl₆, can be used as a simple rule that helps to search for superconductor candidates. In fact, a correlation between antibonding population and superconductivity has been reported for other, chemically distinct systems: NbRuB⁵² and SrSnP,⁵³ for example, and also, e.g., in ThCr₂Si₂type KNi₂S₂ and KNi₂Se₂ compounds.^{49–51} This criterion is useful for the initial screening of superconductor candidates, as it is based only on the crystal structure and the results of relatively simple electronic structural calculations and does not require computationally demanding phonon structure calculations.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.chemmater.9b05277.

Heat capacity of RuAl_6 at T = 2-300 K; XRD pattern of the RuAl_6 sample used for heat capacity measurements; electronic band structures and DOS for RuAl_6 and ReAl_6 in a wider energy range; -COHP curves for HfC and TaC; and resistivity of $M_2\text{Al}_9$ (M = Co, Rh, Ir) (PDF)

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Notes

The authors declare no competing financial interest.

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■ ABBREVIATIONS

COHP, crystal orbital Hamilton population; DOS, density of states; EPC, electron-phonon coupling; FC, field cooling; NN, nearest neighbors; XRD, X-ray diffraction; ZFC, zero-field cooling

REFERENCES

(1) Conder, K. A Second Life of the Matthias's Rules. *Supercond. Sci. Technol.* **2016**, *29*, No. 080502.

(2) Matthias, B. T. The Search for High-temperature Superconductors. *Phys. Today* **1971**, *24*, 23.

(3) Matthias, B. T. Transition Temperatures of Superconductors. *Phys. Rev.* **1953**, *92*, 874–876.

(4) Klimczuk, T.; Wang, C. H.; Gofryk, K.; Ronning, F.; Winterlik, J.; Fecher, G. H.; Griveau, J.-C.; Colineau, E.; Felser, C.; Thompson, J. D.; Safarik, D. J.; Cava, R. J. Superconductivity in the Heusler Family of Intermetallics. *Phys. Rev. B* **2012**, *85*, No. 174505.

(5) von Rohr, F.; Winiarski, M. J.; Tao, J.; Klimczuk, T.; Cava, R. J. Effect of Electron Count and Chemical Complexity in the Ta-Nb-Hf-Zr-Ti High-Entropy Alloy Superconductor. *Proc. Natl. Acad. Sci. U.S.A.* **2016**, *113*, E7144–E7150.

(6) Xie, W.; Luo, H.; Phelan, B. F.; Klimczuk, T.; Cevallos, F. A.; Cava, R. J. Endohedral Gallide Cluster Superconductors and Superconductivity in ReGa5. *Proc. Natl. Acad. Sci. U.S.A.* **2015**, *112*, E7048–E7054.

(7) Shibayama, T.; Nohara, M.; Katori, H. A.; Okamoto, Y.; Hiroi, Z.; Takagi, H. Superconductivity in Rh2Ga9 and Ir2Ga9 without Inversion Symmetry. *J. Phys. Soc. Jpn.* **2007**, *76*, 073708.

(8) Caplin, A. D.; Grüner, G.; Dunlop, J. B. Al10V: An Einstein Solid. *Phys. Rev. Lett.* **1973**, *30*, 1138–1140.

(9) Boström, M.; Rosner, H.; Prots, Y.; Burkhardt, U.; Grin, Y. The Co2Al9 Structure Type Revisited. Z. Anorg. Allg. Chem. 2005, 631, 534–541.

(10) Edshammar, L.-E. The Crystal Structure of RuAl6. Acta Chem. Scand. 1968, 22, 2374–2375.

(11) Peets, D. C.; Cheng, E.; Ying, T.; Kriener, M.; Shen, X.; Li, S.; Feng, D. Type-I Superconductivity in Al6Re. *Phys. Rev. B* 2019, 99, No. 144519.

(12) Cheng, E.; Peets, D. C.; Xi, C.; Huang, Y.; Pi, L.; Li, S. Magnetotransport in Al6Re. *Phys. Rev. B* 2019, *100*, No. 054509.

(13) Mi, S.; Balanetskyy, S.; Grushko, B. A Study of the Al-Rich Part of the Al–Ru Alloy System. *Intermetallics* **2003**, *11*, 643–649.

(14) Rodríguez-Carvajal, J. Recent Advances in Magnetic Structure Determination by Neutron Powder Diffraction. *Phys. B* **1993**, *192*, 55–69.

(15) Canfield, P. C.; Fisk, Z. Growth of Single Crystals from Metallic Fluxes. *Philos. Mag. B* **1992**, 65, 1117–1123.

(16) Kanatzidis, M. G.; Pöttgen, R.; Jeitschko, W. The Metal Flux: A Preparative Tool for the Exploration of Intermetallic Compounds. *Angew. Chem., Int. Ed.* **2005**, *44*, 6996–7023.

(17) Phelan, W. A.; Koohpayeh, S. M.; Cottingham, P.; Tutmaher, J. A.; Leiner, J. C.; Lumsden, M. D.; Lavelle, C. M.; Wang, X. P.; Hoffmann, C.; Siegler, M. A.; Haldolaarachchige, N.; Young, D. P.; McQueen, T. M. On the Chemistry and Physical Properties of Flux and Floating Zone Grown SmB 6 Single Crystals. *Sci. Rep.* **2016**, *6*, No. 20860.

(18) Miccoli, I.; Edler, F.; Pfnür, H.; Tegenkamp, C. The 100th Anniversary of the Four-Point Probe Technique: The Role of Probe Geometries in Isotropic and Anisotropic Systems. J. Phys.: Condens. Matter 2015, 27, No. 223201.

(19) Physical Property Measurement System Helium-3 RefrigeratorSystem User's Manual, 1092-100, Rev. D7. Quantum Design July, 2017.

(20) Hwang, J. S.; Lin, K. J.; Tien, C. Measurement of Heat Capacity by Fitting the Whole Temperature Response of a Heat-Pulse Calorimeter. *Rev. Sci. Instrum.* **1997**, *68*, 94–101.

(21) Physical Property Measurement System Heat Capacity OptionUser's Manual, 1085-150, Rev. M6. Quantum Design February, 2015.

(22) Radebaugh, R.; Siegwarth, J. D. Dilution Refrigerator Technology. Cryogenics 1971, 11, 368-384.

(23) Das, P.; de Ouboter, R. B.; Taconis, K. W. A Realization of a London-Clarke-Mendoza Type Refrigerator. In *Low Temperature Physics LT9*; Daunt, J. G.; Edwards, D. O.; Milford, F. J.; Yaqub, M., Eds.; Springer: Boston, MA, 1965; pp 1253–1255.

(24) Physical Property Measurement System Dilution Refrigerator-User's Manual, 1091-100, Rev. A5. Quantum Design January, 2013.

(25) Dronskowski, R.; Bloechl, P. E. Crystal Orbital Hamilton Populations (COHP): Energy-Resolved Visualization of Chemical Bonding in Solids Based on Density-Functional Calculations. J. Phys. Chem. A 1993, 97, 8617–8624.

(26) Steinberg, S.; Dronskowski, R. The Crystal Orbital Hamilton Population (COHP) Method as a Tool to Visualize and Analyze Chemical Bonding in Intermetallic Compounds. *Crystals* **2018**, *8*, No. 225.

(27) The STUTTGART TB-LMTO-ASA program. https://www2. fkf.mpg.de/andersen/LMTODOC/LMTODOC.html (accessed April 15, 2020).

(28) Skriver, H. L. The LMTO Method: Muffin-Tin Orbitals and Electronic Structure; Springer-Verlag: Berlin; New York, 1984.

(29) Perdew, J. P.; Wang, Y. Accurate and Simple Analytic Representation of the Electron-Gas Correlation Energy. *Phys. Rev. B* **1992**, *45*, 13244–13249.

(30) Perdew, J. P.; Burke, K.; Ernzerhof, M. Generalized Gradient Approximation Made Simple. *Phys. Rev. Lett.* **1996**, *77*, 3865–3868. (31) The Elk Code. http://elk.sourceforge.net (accessed April 15, 2020).

(32) Toby, B. H. R. Factors in Rietveld Analysis: How Good Is Good Enough? *Powder Diffr.* 2006, 21, 67–70.

(33) Huot, J.; Černý, R. Neutron Powder Diffraction. In Neutron Scattering and Other Nuclear Techniques for Hydrogen in Materials. In *Neutron Scattering Applications and Techniques*; Fritzsche, H.; Huot, J.; Fruchart, D., Eds.; Springer International Publishing, 2016; pp 31– 89.

(34) Klimczuk, T.; Cava, R. J. Carbon Isotope Effect in Superconducting MgCNi3. *Phys. Rev. B* 2004, *70*, No. 212514.

(35) Prozorov, R.; Kogan, V. G. Effective Demagnetizing Factors of Diamagnetic Samples of Various Shapes. *Phys. Rev. Appl.* **2018**, *10*, No. 014030.

(36) Powell, R. L.; Clark, A. F. Definitions of Terms for Practical Superconductors. 2. Critical Parameters. *Cryogenics* 1978, 18, 137–141.

(37) Fickett, F. R. Standards for Measurement of the Critical Fields of Superconductors. J. Res. Natl. Bur. Stand. **1985**, 90, 95–113.

(38) Klimczuk, T.; Szlawska, M.; Kaczorowski, D.; O'Brien, J. R.; Safarik, D. J. Superconductivity in the Einstein Solid V Al 10.1. *J. Phys.: Condens. Matter* **2012**, *24*, No. 365701.

(39) Winiarski, M. J.; Wiendlocha, B.; Sternik, M.; Wiśniewski, P.; O'Brien, J. R.; Kaczorowski, D.; Klimczuk, T. Rattling-Enhanced Superconductivity in MV2Al20 (M=Sc, Lu, Y) Intermetallic Cage Compounds. *Phys. Rev. B* **2016**, *93*, No. 134507.

(40) Micnas, R.; Ranninger, J.; Robaszkiewicz, S. Superconductivity in Narrow-Band Systems with Local Nonretarded Attractive Interactions. *Rev. Mod. Phys.* **1990**, *62*, 113–171.

(41) Tinkham, M. Introduction to Superconductivity; McGraw Hill: New York, 1996.

(42) Charles, K. Introduction to Solid State Physics, 8th ed.; Wiley: Hoboken, 2004.

(43) Werthamer, N. R.; Helfand, E.; Hohenberg, P. C. Temperature and Purity Dependence of the Superconducting Critical Field, Hc2. III. Electron Spin and Spin-Orbit Effects. *Phys. Rev.* **1966**, *147*, 295– 302.

(44) Cyrot, M.; Pavuna, D.Introduction to Superconductivity and High-Tc Materials; World Scientific, 1992.

(45) McMillan, W. L. Transition Temperature of Strong-Coupled Superconductors. *Phys. Rev.* **1968**, *167*, 331–344.

(46) Dronskowski, R.; Korczak, K.; Lueken, H.; Jung, W. Chemically Tuning between Ferromagnetism and Antiferromagnetism by Combining Theory and Synthesis in Iron/Manganese Rhodium Borides. *Angew. Chem., Int. Ed.* **2002**, *41*, 2528–2532.

(47) Decker, A.; Landrum, G. A.; Dronskowski, R. Structural and Electronic Peierls Distortions in the Elements (A): The Crystal Structure of Tellurium. *Z. Anorg. Allg. Chem.* **2002**, *628*, 295–302.

(48) Fokwa, B. P. T.; Lueken, H.; Dronskowski, R. Rational Synthetic Tuning between Itinerant Antiferromagnetism and Ferromagnetism in the Complex Boride Series Sc2FeRu5–nRhnB2 ($0 \le n \le 5$). Chem. - Eur. J. 2007, 13, 6040–6046.

(49) Neilson, J. R.; McQueen, T. M. Bonding, Ion Mobility, and Rate-Limiting Steps in Deintercalation Reactions with ThCr2Si2-Type KNi2Se2. J. Am. Chem. Soc. **2012**, 134, 7750–7757.

(50) Neilson, J. R.; Llobet, A.; Stier, A. V.; Wu, L.; Wen, J.; Tao, J.; Zhu, Y.; Tesanovic, Z. B.; Armitage, N. P.; McQueen, T. M. Mixed-Valence-Driven Heavy-Fermion Behavior and Superconductivity in KNi2Se2. *Phys. Rev. B* **2012**, *86*, No. 054512.

(51) Neilson, J. R.; McQueen, T. M.; Llobet, A.; Wen, J.; Suchomel, M. R. Charge Density Wave Fluctuations, Heavy Electrons, and Superconductivity in KNi2S2. *Phys. Rev. B* **2013**, *87*, No. 045124.

(52) Xie, W.; Luo, H.; Baroudi, K.; Krizan, J. W.; Phelan, B. F.; Cava, R. J. Fragment-Based Design of NbRuB as a New Metal-Rich Boride Superconductor. *Chem. Mater.* **2015**, *27*, 1149–1152.

(53) Gui, X.; Sobczak, Z.; Chang, T.-R.; Xu, X.; Huang, A.; Jia, S.; Jeng, H.-T.; Klimczuk, T.; Xie, W. Superconducting SrSnP with Strong Sn-P Antibonding Interaction: Is the Sn Atom Single or Mixed Valent? *Chem. Mater.* **2018**, *30*, 6005–6013.

(54) Grin, Y.; Wedig, U.; Wagner, F.; von Schnering, H. G.; Savin, A. The Analysis of "Empty Space" in the PdGa5 Structure. *J. Alloys Compd.* **1997**, 255, 203–208.

(55) Okamoto, H. Al-Rh (Aluminum-Rhodium). J. Phase Equilib. Diffus. 2007, 28, 485.

(56) Allen, P. B.; Cohen, M. L. Superconductivity and Phonon Softening. *Phys. Rev. Lett.* **1972**, *29*, 1593–1596.

(57) Yannello, V. J.; Fredrickson, D. C. Orbital Origins of Helices and Magic Electron Counts in the Nowotny Chimney Ladders: The 18 – n Rule and a Path to Incommensurability. *Inorg. Chem.* **2014**, *53*, 10627–10631.

(58) Yannello, V. J.; Fredrickson, D. C. Generality of the 18-n Rule: Intermetallic Structural Chemistry Explained through Isolobal Analogies to Transition Metal Complexes. *Inorg. Chem.* **2015**, *54*, 11385–11398.

(59) Miyazaki, K.; Yannello, V. J.; Fredrickson, D. C. Electron-Counting in Intermetallics Made Easy: The 18-n Rule and Isolobal Bonds across the Os–Al System. *Z. Kristallogr. - Cryst. Mater.* **2017**, 232, 487–496.

(60) Slater, J. C. Atomic Radii in Crystals. J. Chem. Phys. 1964, 41, 3199–3204.

(61) Cordero, B.; Gómez, V.; Platero-Prats, A. E.; Revés, M.; Echeverría, J.; Cremades, E.; Barragán, F.; Alvarez, S. Covalent Radii Revisited. *Dalton Trans.* **2008**, *21*, 2832–2838.

(62) Verchenko, V. Y.; Mironov, A. V.; Wei, Z.; Tsirlin, A. A.; Dikarev, E. V.; Shevelkov, A. V. Crystal Growth of Intermetallics from the Joint Flux: Exploratory Synthesis through the Control of Valence Electron Count. *Inorg. Chem.* **2019**, *58*, 1561–1570.

(63) Bradlyn, B.; Elcoro, L.; Cano, J.; Vergniory, M. G.; Wang, Z.; Felser, C.; Aroyo, M. I.; Bernevig, B. A. Topological Quantum Chemistry. *Nature* **2017**, *547*, 298–305. (64) Vergniory, M. G.; Elcoro, L.; Felser, C.; Regnault, N.; Bernevig, B. A.; Wang, Z. A Complete Catalogue of High-Quality Topological Materials. *Nature* **2019**, *566*, 480–485.

(65) Topological Materials Database. https://www. topologicalquantumchemistry.org/#/detail/58157 (accessed April 15, 2020).

(66) Zhang, T.; Jiang, Y.; Song, Z.; Huang, H.; He, Y.; Fang, Z.; Weng, H.; Fang, C. Catalogue of Topological Electronic Materials. *Nature* **2019**, *566*, 475–479.

(67) Topological properties and more for material Al6Ru (sg63)| Materiae. http://materiae.iphy.ac.cn/materials/MAT00012610 (accessed April 15, 2020).

(68) Simon, A. Superconductivity and the Periodic Table: From Elements to Materials. *Philos. Trans. R. Soc., A* 2015, 373, No. 20140192.

(69) Mauri, F.; Zakharov, O.; de Gironcoli, S.; Louie, S. G.; Cohen, M. L. Phonon Softening and Superconductivity in Tellurium under Pressure. *Phys. Rev. Lett.* **1996**, *77*, 1151–1154.

(70) Kusmartseva, A. F.; Sipos, B.; Berger, H.; Forró, L.; Tutiš, E. Pressure Induced Superconductivity in Pristine 1T-TiSe2. *Phys. Rev. Lett.* **2009**, *103*, No. 236401.