HAT-P-50b, HAT-P-51b, HAT-P-52b, AND HAT-P-53b: THREE TRANSITING HOT JUPITERS AND A TRANSITING HOT SATURN FROM THE HATNET SURVEY*

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ABSTRACT

We report the discovery and characterization of four transiting exoplanets by the HATNet survey. The planet HATP-50b has a mass of $1.35~M_{\rm J}$ and radius of $1.29~R_{\rm J}$, and orbits a bright ($V=11.8~{\rm mag}$) $M=1.27~M_{\odot}$, $R=1.70~R_{\odot}$ star every $P=3.1220~{\rm days}$. The planet HAT-P-51b has a mass of $0.31~M_{\rm J}$ and radius of $1.29~R_{\rm J}$, and orbits a $V=13.4~{\rm mag}$, $M=0.98~M_{\odot}$, $R=1.04~R_{\odot}$ star with a period of $P=4.2180~{\rm days}$. The planet HAT-P-52b has a mass of $0.82M_{\rm J}$ and radius of $1.01~R_{\rm J}$, and orbits a $V=14.1~{\rm mag}$, $M=0.89~M_{\odot}$, $R=0.89~R_{\odot}$ star with a period of $P=2.7536~{\rm days}$. The planet HAT-P-53b has a mass of $1.48~M_{\rm J}$ and radius of $1.32~R_{\rm J}$, and orbits a $V=13.7~{\rm mag}$, $M=1.09~M_{\odot}$, $R=1.21~R_{\odot}$ star with a period of $P=1.9616~{\rm days}$. All four planets are consistent with having circular orbits and have masses and radii measured to better than 10% precision. The low stellar jitter and favorable R_p/R_{\star} ratio for HAT-P-51 make it a promising target for measuring the Rossiter–McLaughlin effect for a Saturn-mass planet.

Key words: planetary systems – stars: individual (HAT-P-50, HAT-P-51, HAT-P-52, HAT-P-53) – techniques: photometric – techniques: spectroscopic

Supporting material: machine-readable and VO table

1. INTRODUCTION

Transiting exoplanets (TEPs) are important objects for studying the physical properties of planets outside the solar system. By combining time-series photometry of a transit with time-series radial velocity (RV) observations of the star spanning the planetary orbit, it is possible to accurately measure the mass and radius of a transiting planet relative to those of the host star. Leveraging stellar evolution models to

estimate the stellar mass and radius given observable parameters such as the effective temperature, metallicity and bulk density of the star, then allows the physical mass and radius of the planet, as well as its orbital separation, to be determined. Other properties of the system such as the orbital eccentricity and obliquity (e.g., Queloz et al. 2000), and properties of the planetary atmosphere (e.g., emission or transmission spectra) may also be accessible for transiting planets (e.g., Charbonneau et al. 2002). Motivated by the wealth of physical information that may be measured for these objects, there has been a significant effort over the past 15 years to discover and characterize many TEPs. The aim of this effort is to explore the diversity of exoplanets, and to identify statistically robust relations between their physical parameters, which in turn inform theories of planet formation and evolution (e.g., Guillot et al. 2006; Burrows et al. 2007; Béky et al. 2011; Laughlin et al. 2011; Enoch et al. 2012).

Largely thanks to the ultra-high-precision photometric timeseries observations from the NASA *Kepler* mission, we now know of over 4000 high-quality *candidate* transiting exoplanets (e.g., Mullally et al. 2015). Some 51 of the *Kepler* candidates have been confirmed through measuring the RV orbital wobble of their host stars, while a further 845 have masses estimated

^{*}Based on observations obtained with the Hungarian-made Automated Telescope Network. Based on observations obtained at the W. M. Keck Observatory, which is operated by the University of California and the California Institute of Technology. Keck time has been granted by NOAO (A245Hr) and NASA (N154Hr, N130Hr). Based on data collected at Subaru Telescope, which is operated by the National Astronomical Observatory of Japan. Based on observations made with the Nordic Optical Telescope, operated on the island of La Palma jointly by Denmark, Finland, Iceland, Norway, Sweden, in the Spanish Observatorio del Roque de los Muchachos of the Instituto de Astrofísica de Canarias. Based on observations obtained with the Tillinghast Reflector 1.5 m telescope and the 1.2 m telescope, both operated by the Smithsonian Astrophysical Observatory at the Fred Lawrence Whipple Observatory in AZ. Based on radial velocities obtained with the Sophie spectrograph mounted on the 1.93 m telescope at Observatoire de Haute-Provence. Based on observations obtained with facilities of the Las Cumbres Observatory Global Telescope.

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through transit time variations, or have been statistically validated as being very unlikely to be anything other than transiting planets. The majority of the candidates from *Kepler* are, however, too small and/or orbiting stars that are too faint to allow their masses and orbital eccentricities to be determined using existing spectroscopic facilities. For most of these planets, all we can determine at present are their radii, orbital periods, and a constraint on their eccentricities using the so-called photo-eccentric effect (e.g., Dawson & Johnson 2012).

Most of the TEPs with spectroscopically determined masses have been discovered by wide-field ground-based transit surveys such as HATNet (Bakos et al. 2004), HATSouth (Bakos et al. 2013), WASP (Pollacco et al. 2006), XO (McCullough et al. 2005), TrES (Alonso et al. 2004), and KELT (Pepper et al. 2007), among others. These surveys cover a greater area of the sky than has been surveyed so far by *Kepler* or its successor mission *K2*, and have thereby monitored more bright stars which may host TEPs amenable to confirmation spectroscopy. In this paper we present the discovery and characterization of four new transiting short-period gas-giant planets by the HATNet survey.

The HATNet survey, which began operations in 2004, has to date searched 17% of the 4π steradian celestial sphere for planets. A total of 5.5 million stars have been observed. The stars have from 2400 to 21,000 high-cadence photometric observations (5th and 95th percentiles; the median is 7200) spanning a few months to several years. The point-to-point rms precision of the observations ranges from \sim 3 mmag for stars with $r \sim 9$ to $\sim 2\%$ for stars with $r \sim 13.3$ (depending on sky conditions and the density of stars in the field being observed). Based on these observations we have identified ~2000 candidate TEPs, the majority of which are false positives (the transit signal is probably real, but not due to a planet), or false alarms (the identified transit signal was not real). Approximately 96% of the fully vetted candidates have been rejected as either a false positive or a false alarm. As most false positives can be quickly rejected from a handful of follow-up observations, while planets may remain active for a long time before they are fully confirmed, this fraction is an upper limit on the true fraction of false positives and false alarms in our full sample of candidates. The stars are generally bright (the median magnitude of the candidates is V = 12.7 mag) so that it has been possible to carry out spectroscopic and/or photometric follow-up observations for the majority of these objects. Based on this follow-up, 1468 candidates have been rejected as false positives, 189 have been rejected as false alarms, while more than 50 confirmed and well-characterized planets (including those presented here) have been announced. Some \sim 350 candidates are currently active.

The four new planets announced in this paper have properties that are typical of short-period gas-giant planets. While they do not, in themselves, reveal new properties of exoplanets, they will contribute to our statistical understanding of planetary systems in the Galaxy.

In the next section we describe the observations used to confirm the new TEPs. In Section 3 we discuss the analysis carried out to rule out false positive blend scenarios and determine the physical parameters of the planetary systems. We place these planets into context with the other known transiting planets in Section 4.

2. OBSERVATIONS

The discovery of all four transiting planet systems followed the general observational procedures described by Latham et al. (2009) and Bakos et al. (2010). Here we summarize the observations of each system, and our methods for reducing the raw data to scientifically interesting measurements.

2.1. Photometric Detection

The four TEPs presented here were initially identified as candidate TEPs based on observations made with the HATNet wide-field photometric instruments (Bakos et al. 2004). This network consists of six identical fully automated instruments, with four at Fred Lawrence Whipple Observatory (FLWO) in AZ, and two on the roof of the Submillimeter Array Hangar Building at Mauna Kea Observatory (MKO) in HI. The lightgathering elements of each instrument include an 11 cm diameter telephoto lens, a Sloan r filter, and a $4K \times 4K$ front-side-illuminated CCD camera. Observations made in 2007 and early 2008 were carried out using a Cousins R filter. The instruments have a field of view of $10^{\circ}.6 \times 10^{\circ}.6$ and a pixel scale of 9'' pixel⁻¹ at the center of an image. Observations are fully automated with the typical procedure being to continuously monitor a given field while it is above 30° elevation taking exposures of 180 s (prior to 2010 December an exposure time of 300 s was used). The fields have been defined by tiling the sky into 838 $7^{\circ} \times 7^{\circ}$ pointings. Because each tile is smaller than the field of view, there is overlap between neighboring fields and a given source may be observed in multiple (up to four) fields.

Table 1 lists the HATNet observations which contributed to the discovery of each system. All four objects were observed using multiple HAT instruments, and three of the four objects are in overlapping fields. In some cases the observations date back to 2007, and may span as many as 3.5 years. HAT-P-51, in particular, has been observed extensively with HATNet, having more than 27,000 individual photometric measurements.

The raw HATNet images were reduced to systematic-noisefiltered light curves following Bakos et al. (2010) and making use of aperture and image subtraction photometry tools from Pál (2009). The filtering includes decorrelating the individual light curves against various instrumental parameters (we refer to this procedure as External Parameter Decorrelation, or EPD) including the image position of the source, the sub-pixel position, the background flux, the local scatter in the background flux, and the shape of the point-spread function. Following EPD we make use of the Trend Filtering Algorithm (TFA; Kovács et al. 2005) in non-reconstructive mode. The data for each HATNet field were reduced independently, with EPD applied separately to each instrument, and TFA applied globally to all observations from a given field (with an option to perform a complete TFA filtering, using data from all telescopes and all fields).

Light curves were searched for periodic box-shaped transits using the Box-fitting Least Squares algorithm (BLS; Kovács et al. 2002). Candidates were selected using a variety of automated cuts (e.g., on the signal-to-noise ratio; S/N, differences in depth between even and odd transits, among others) and a final by-eye inspection. Figure 1 shows the phase-folded, trend-filtered light curves from HATNet for the four newly discovered planetary systems.

¹⁶ http://exoplanets.org accessed 2015 February 18.

 Table 1

 Summary of Photometric Observations

Instrument/Field ^a	Date(s)	# Images	Cadence ^b	Filter	Precision ^c
			(s)		(mmag)
HAT-P-50					
HAT-10/G316	2008 Nov-2009 May	3214	352	Sloan r	7.5
HAT-5/G364	2009 May	21	411	Sloan r	10.6
HAT-9/G364	2008 Dec-2009 May	3159	352	Sloan r	7.5
BOS	2012 Feb 15	105	149	Sloan i	2.1
Keplercam	2012 Feb 18	443	54	Sloan i	1.2
BOS	2012 Feb 21	81	140	Sloan i	2.5
BOS	2012 Apr 08	61	143	Sloan i	1.6
Keplercam	2012 Nov 28	462	44	Sloan i	1.8
Keplercam	2012 Dec 23	277	45	Sloan i	2.3
Keplercam	2013 Jan 14	427	45	Sloan i	1.4
Keplercam	2013 Jan 17	380	45	Sloan i	1.6
HAT-P-51					
HAT-6/G164	2007 Sep-2008 Feb	3652	349	Cousins R	30.3
HAT-9/G164	2007 Sep-2008 Feb	2767	349	Cousins R	25.9
HAT-10/G165	2010 Sep-2011 Jan	4215	230	Sloan r	24.3
HAT-5/G165	2010 Nov-2011 Feb	4142	354	Sloan r	24.1
HAT-8/G165	2010 Nov-2011 Feb	2240	238	Sloan r	23.6
HAT-6/G209	2010 Nov-2011 Feb	3794	351	Sloan r	18.4
HAT-9/G209	2010 Nov-2011 Feb	2151	352	Sloan r	18.0
HAT-7/G210	2010 Nov-2011 Jan	4047	229	Sloan r	19.1
Keplercam	2011 Oct 21	88	134	Sloan i	1.9
Keplercam	2012 Jan 05	92	133	Sloan i	2.7
Keplercam	2012 Oct 05	171	134	Sloan i	2.2
Keplercam	2012 Oct 26	137	134	Sloan i	2.6
Keplercam	2012 Nov 12	111	134	Sloan i	3.2
HAT-P-52					
HAT-5/G212	2010 Sep-Nov	2270	347	Sloan r	19.5
HAT-8/G212	2010 Aug–Nov	5999	232	Sloan r	22.4
Keplercam	2010 Dec 23	101	134	Sloan i	2.0
Keplercam	2011 Sep 05	90	133	Sloan i	2.7
Keplercam	2011 Sep 27	188	134	Sloan i	2.3
Keplercam	2011 Nov 21	82	133	Sloan i	2.5
Keplercam	2012 Jan 07	64	194	Sloan i	3.0
HAT-P-53					
HAT-6/G164	2007 Sep-2008 Feb	3653	349	Cousins R	26.4
HAT-9/G164	2007 Sep–2008 Feb	2764	349	Cousins R	24.5
HAT-10/G165	2010 Sep–2011 Jan	4234	230	Sloan r	19.3
HAT-5/G165	2010 Nov-2011 Feb	4134	354	Sloan r	19.4
HAT-8/G165	2010 Nov-2011 Feb	2240	238	Sloan r	20.4
Keplercam	2011 Oct 19	158	134	Sloan i	1.9
Keplercam	2011 Oct 19 2011 Oct 27	381	73	Sloan i	2.5

We used BLS to search the residual light curves for additional planetary transits, but did not detect any additional signals. We also calculated the Discrete Fourier Transform (DFT, see Deeming 1975, and using the method of Kurtz 1985 for a fast recursive evaluation of the trigonometric functions) for each of the light curves, after subtracting the best-fit transit models, to search for any continuous periodic variations. Such variations may be due to the rotation of spotted stars, for example. For HAT-P-50, -52 and -53 we can rule out signals in

the frequency range $0-50\,\mathrm{d}^{-1}$ with an amplitude above 0.6 mmag, 1.3 mmag and 1.3 mmag, respectively. For HAT-P-51 we also do not find a significant Fourier component. Curiously, the highest peak in the frequency spectrum is within 1.3% of the first harmonic of the orbital frequency. We do not have a physical explanation of this near coincidence, if it is a real signal, but we can exclude the possibility of tidal distortion due to the well-demonstrated sub-stellar nature of the companion (see Section 3.3). It may perhaps be a signature

^a For HATNet data we list the HAT station and field name from which the observations are taken. HAT-5, -6, -7, and -10 are located at FLWO in Arizona, while HAT-8 and -9 are located at MKO in Hawaii. Each field corresponds to one of 838 fixed pointings used to cover the full 4π celestial sphere. All data from a given HATNet field are reduced together, while detrending through External Parameter Decorrelation (EPD) is done independently for each unique field+station combination.

^b The mode time between consecutive images rounded to the nearest second. Due to weather, the day–night cycle, guiding and focus corrections, and other factors, the cadence is only approximately uniform over short timescales.

^c The rms of the residuals from the best-fit model.

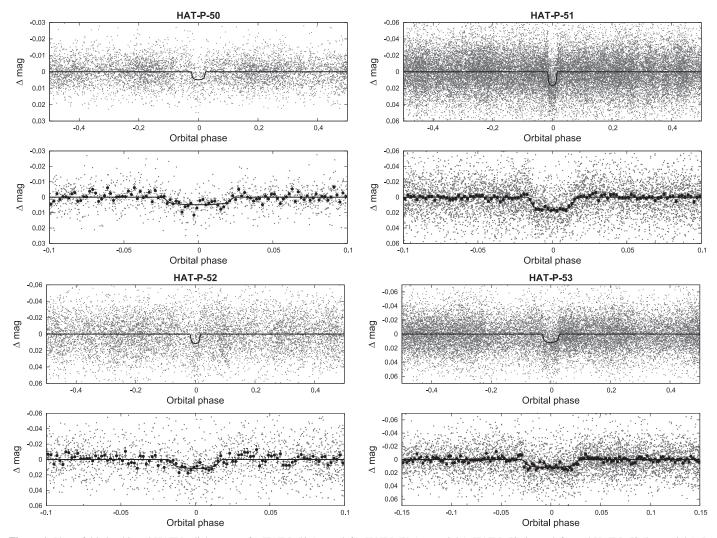


Figure 1. Phase-folded unbinned HATNet light curves for HAT-P-50 (upper left), HAT-P-51 (upper right), HAT-P-52 (lower left), and HAT-P-53 (lower right). In each case we show two panels. The top panel shows the full light curve, while the bottom panel shows the light curve zoomed-in on the transit. The solid lines show the model fits to the light curves. The dark filled circles in the bottom panels show the light curves binned in phase with a bin size of 0.002 in phase.

of stellar activity. After subtracting this low amplitude (1.3 mmag) component, the next highest peak in the frequency spectrum has an amplitude of 1.0 mmag.

2.2. Spectroscopic Observations

Follow-up spectroscopic observations were carried out using six different facilities. The aim of these observations was to aid in ruling out false positives, determine the atmospheric parameters of the host stars, and to confirm the planets by measuring the RV orbital variations induced by the transiting planets. The facilities used for each system are summarized in Table 2, and include the Tillinghast Reflector Echelle Spectrograph (TRES; Fűresz 2008) on the 1.5 m Tillinghast Reflector at FLWO; the Astrophysical Research Consortium Echelle Spectrometer (ARCES; Wang et al. 2003) on the ARC 3.5 m telescope at Apache Point Observatory (APO) in New Mexico; the FIbre-fed Échelle Spectrograph (FIES) at the 2.5 m Nordic Optical Telescope (NOT) at La Palma, Spain (Djupvik & Andersen 2010); the SOPHIE Spectrograph on the 1.93 m telescope at OHP (Bouchy et al. 2009) in France; HIRES (Vogt et al. 1994) on the Keck-I telescope in Hawaii together with the I_2 absorption cell; and the High-Dispersion Spectrograph (HDS; Noguchi et al. 2002) with the I_2 absorption cell (Kambe et al. 2002) on the Subaru telescope in Hawaii.

The TRES observations were used for reconnaissance (i.e., ruling out false positives with lower S/N spectra) for HAT-P-51, HAT-P-52 and HAT-P-53. For HAT-P-50 they were used both for reconnaissance and for measuring the orbital variation due to the planet. The raw echelle images were reduced to extracted spectra and analyzed to measure RVs and stellar atmospheric parameters following Buchhave et al. (2010). Observations of standard stars were made during each observing run and are used to correct the velocities from each run to the IAU system. Because these corrections are known for TRES, we adopt the TRES measurements for the systemic γ velocity of each object listed in Table 3. The uncertainty on the absolute calibration is $\sim\!\!0.1\,\mathrm{km}\,\mathrm{s}^{-1}$ and is dominated by the uncertainty in the absolute velocities of the standard stars.

The ARCES observations of HAT-P-51 and HAT-P-53 were used exclusively for reconnaissance (based on observations of standard stars the RV precision of this instrument is limited to \sim 500 m s⁻¹). Observations were reduced to wavelength

Table 2
Summary of Spectroscopy Observations

Instrument	Date(s)	# Spec.	Res. $\Delta \lambda / \lambda / 1000$	S/N Range ^a	RV Precision ^b (m s ⁻¹)
HAT-P-50			Δλ/ λ/ 1000		(111.5)
TRES	2010 Dec-2012 Feb	5	44	24.8–36.1	116.0
FIES	2010 Dec=2012 Feb 2012 Mar 13–17	5	67	31.0–69.9	25.0
HDS	2012 Wai 13–17 2012 Feb 7	3	60	271–283	23.0
HDS+I2	2012 Feb / 2012 Feb—Sep	20	60	84–166	23.0
HAT-P-51	2012 Геб–Зер	20	00	84–100	23.0
FIES	2011 Ang 4	1	46	27.4	
	2011 Aug 4	1			•••
ARCES	2011 Sep 19	1	31.5	20.6	•••
TRES	2011 Sep 21	1	44	20.9	•••
SOPHIE	2011 Dec 4–12	4	39	23–28	37
HIRES	2011 Oct-Nov	2	55	83–94	•••
HIRES+I2	2011 Oct-2012 Feb	6	55	59–80	5.4
HDS	2012 Feb 9	4	60	52–56	
HDS+I2	2012 Feb 7-10	20	60	26–53	9.2
HAT-P-52					
TRES	2010 Dec-2011 Jan	2	44	19.1–20.4	300
HIRES	2011 Oct 19	1	55	66	
HIRES+I2	2011 Feb-2012 Jul	7	55	26–59	7.5
HAT-P-53					
TRES	2011 Sep 18-19	2	44	30.6-30.7	80
ARCES	2011 Sep 19–20	2	31.5	19.8–20.1	380
HIRES	2011 Nov 14	1	55	90	
HIRES+I2	2011 Nov 14 2011 Nov-2012 Feb	6	55	62–79	11.0

calibrated spectra using the ECHELLE package in IRAF. ¹⁷ For the wavelength calibration we made use of ThAr lamp spectra obtained before or after each science exposure, and with the same pointing as the science exposure. Each spectrum was analyzed to measure the RV of the star, its surface gravity, effective temperature, projected equatorial rotation velocity, and metallicity using the Stellar Parameter Classification (SPC; Buchhave et al. 2012) procedure, which cross-correlates the observed spectrum against a set of synthetic template spectra.

The single FIES spectrum obtained for HAT-P-51 was used for reconnaissance, and was reduced and analyzed following Buchhave et al. (2010).

SOPHIE observations of HAT-P-51 were collected in high-efficiency mode with the aim of confirming the planet by measuring the RV orbital wobble of its host star. The SOPHIE observations were reduced and analyzed following Boisse et al. (2013). Based on these observations we determined that HAT-P-51b is a Saturn-mass planet, and that the ~40 m s⁻¹ precision of the SOPHIE observations for this object was insufficient to accurately determine the planetary mass. The precision in this case was limited due to significant contamination from scattered moon light, for uncontaminated spectra significantly higher precision may be obtained from the same S/N. We do not include these data in the analysis of HAT-P-51.

HDS observations were collected for HAT-P-50 and HAT-P-51 in order to confirm these TEP systems and characterize the planetary orbits. The observations were extracted and reduced

to relative RVs in the solar system barycentric frame following Sato et al. (2002, 2012), while spectral line bisector spans (BSs) were computed following Torres et al. (2007).

HIRES observations were collected for HAT-P-51, HAT-P-52 and HAT-P-53. The observations have an RV precision of $5-10 \text{ m s}^{-1}$ and are used here to characterize the orbital variations and to determine the stellar atmospheric parameters. The data were reduced to relative RVs in the barycentric frame following Butler et al. (1996). Spectral-line BSs were computed following Torres et al. (2007), and *S* activity indices were calculated following Isaacson & Fischer (2010). These were transformed to $\log_{10} R'_{HK}$ values following Noyes et al. (1984).

Based on the reconnaissance TRES, FIES and ARCES observations we find that none of the four targets shows evidence of being a composite system. All have RV variations below $1\,\mathrm{km}\,\mathrm{s}^{-1}$, and all are dwarf stars. The effective temperatures, projected rotation velocities, and surface gravities estimated from these spectra are consistent with the higher precision values presented in Table 3.

The high-precision RV measurements for all objects are seen to vary in phase with the transit ephemerides. These are shown in Figure 2. In this same figure we also show the phased BS measurements, which in all cases are consistent with no variation in phase with the ephemerides. The data are listed in Table 4.

2.3. Photometric Follow-up Observations

Additional time-series photometric measurements were obtained for all four of the systems using Keplercam on the FLWO 1.2 m telescope. These observations were carried out

^a The signal-to-noise ratio per resolution element near 5180 Å.

^b The rms of the RV residuals from the best-fit orbit, or the rms of the RVs for reconnaissance observations. We do not give an estimate for template spectra (listed as HIRES or HDS without I2 included), or for cases where only a single spectrum was obtained with a given instrument.

¹⁷ IRAF is distributed by the National Optical Astronomy Observatories, which are operated by the Association of Universities for Research in Astronomy, Inc., under cooperative agreement with the National Science Foundation.

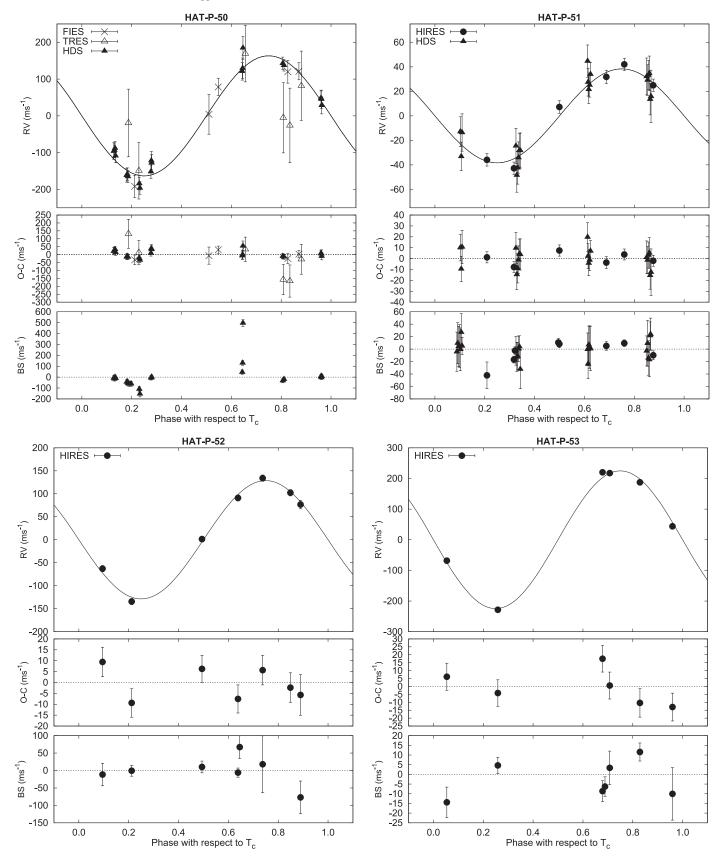


Figure 2. Phased high-precision RV measurements for HAT-P-50 (upper left), HAT-P-51 (upper right), HAT-P-52 (lower left), and HAT-P-53 (lower right). In each case we show three panels. The top panel shows the phased measurements together with our best-fit model (see Table 6) for each system. Zero-phase corresponds to the time of mid-transit. The center-of-mass velocity has been subtracted. The second panel shows the velocity O-C residuals from the best fit. The error bars include the jitter terms listed in Table 6 added in quadrature to the formal errors for each instrument. The third panel shows the bisector spans (BS), with the mean value subtracted. The symbols used for each instrument are indicated in the top panel for each planet. Note the different vertical scales of the panels.

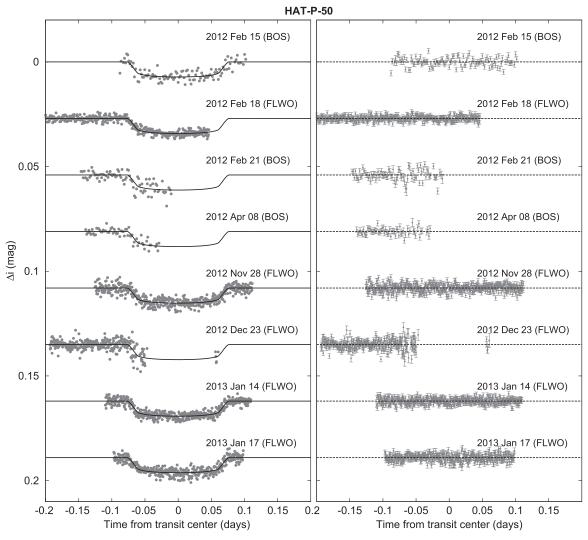


Figure 3. Left: unbinned transit light curves for HAT-P-50, acquired with the CCD imager on the BOS 0.8 m telescope, and Keplercam on the FLWO 1.2 m telescope. The light curves have been EPD and TFA processed, as described in Section 3.1. The dates of the events and instruments used are indicated. Curves after the first are displaced vertically for clarity. Our best fit from the global modeling described in Section 3.1 is shown by the solid lines. Right: residuals from the fits in the same order as the left panel. The error bars represent the photon and background shot noise, plus the readout noise.

during the planetary transits to aid in ruling out blended eclipsing binary false positive scenarios, and to refine the light curve parameters (i.e., the orbital period, the planet to star radius ratio, the impact parameter and the transit duration). For HAT-P-50 we also obtained follow-up photometry with the CCD imager on the Byrne Observatory at Sedgwick (BOS) 0.8 m telescope, located at Sedgwick Reserve in Santa Ynez Valley, CA, and operated by the Las Cumbres Observatory Global Telescope institute (LCOGT; Brown et al. 2013). The events monitored with each instrument, together with the number of images obtained, the cadence, filter used and photometric precision are listed in Table 1.

We applied standard CCD calibration procedures to the Keplercam and BOS images and then reduced these to light curves using the aperture photometry methods described by Bakos et al. (2010). In doing this we made use of the stellar centroid positions measured directly from a set of registered and stacked frames rather than relying on catalog positions for astrometry as done in Bakos et al. (2010). All sources in the images, save the target TEP system, were used in performing the ensemble magnitude calibration. We corrected for

additional systematic trends in the data by including the EPD and TFA noise filtering models in the fitting mentioned in Section 3.1. The resulting trend filtered light curves for HAT-P-50 through HAT-P-53 are shown in Figures 3–6, respectively. All photometric measurements made for the four objects are available in machine-readable form in Table 5.

3. ANALYSIS

3.1. Global Modeling of the Data

We modeled the HATNet photometry, the follow-up photometry, and the high-precision RV measurements using the procedure described in detail by Pál et al. (2008) and Bakos et al. (2010) with modifications described by Hartman et al. (2012). This procedure makes use of the differential evolution Markov Chain Monte Carlo (DEMCMC) method (ter Braak 2006; Eastman et al. 2013) to explore the fitness landscape and produce posterior parameter distributions.

The light curves are modeled using a Mandel & Agol (2002) semi-analytic transit model, with fixed quadratic limb darkening coefficients taken from the tabulation by Claret (2004) for

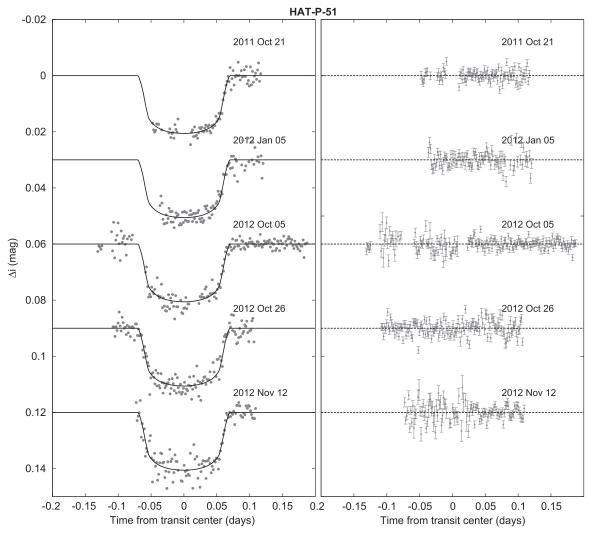


Figure 4. Similar to Figure 3; here we show the follow-up light curves for HAT-P-51. All light curves were obtained with Keplercam on the FLWO 1.2 m telescope.

the stellar atmospheric parameters determined in Section 3.2. For the HATNet photometry we allowed for dilution of the transit signal to account for blending from neighboring stars in the low spatial resolution HATNet images, as well as an artificial reduction of the transit depth due to filtering with TFA before fitting the transit. For the follow-up photometry we included the EPD and TFA instrumental trend models directly in the fit to account for trends that are not calibrated out through our standard ensemble differential photometry routines. Fitting these simultaneously with the transit model preserves the transit shape and allows the uncertainties in the trends to contribute to the uncertainties in the physical parameters.

The RVs are modeled using a standard Keplerian orbit, including RV jitter terms which we added in quadrature to the "formal" RV errors. We varied the jitter values as free parameters in the fits following Hartman et al. (2014), and adopted independent jitters for each instrument as the methods for estimating the formal errors differ between reduction methods and instruments. For HIRES we made use of an empirical prior on the jitter as discussed in Hartman et al. (2014), while for the other instruments we used a Jeffreys prior (i.e., the prior probability for parameter σ is $\propto 1/\sigma$).

The resulting parameters for each system are listed in Table 6, where some parameters such as the planetary masses and radii depend on the stellar parameters, the determination of which is described below in Section 3.2. As discussed in that section, other dependencies on the stellar parameters result from filtering the Markov Chains to restrict them to regions of parameter space covered by stellar evolution models, and iterating between determining the stellar atmospheric parameters and modeling other observations.

We find that HAT-P-50b is a hot Jupiter with a mass of $1.350 \pm 0.073 \, M_{\rm J}$ and radius of $1.288 \pm 0.064 \, R_{\rm J}$, HAT-P-51b is a hot Saturn with a mass of $0.309 \pm 0.018 \, M_{\rm J}$ and radius of $1.293 \pm 0.054 \, R_{\rm J}$, while HAT-P-52b and HAT-P-53b are hot Jupiters with masses of $0.818 \pm 0.029 \, M_{\rm J}$ and $1.484 \pm 0.056 \, M_{\rm J}$, and radii of $1.009 \pm 0.072 \, R_{\rm J}$ and $1.318 \pm 0.091 \, R_{\rm J}$, respectively. We fit all systems both allowing the eccentricity to vary and fixing it to zero. We find that all four systems are consistent with no eccentricity (the 95% confidence upper limits on the eccentricity when it is allowed to vary are e < 0.115, < 0.123, < 0.047, and < 0.134 for HAT-P-50b through HAT-P-53b, respectively). We therefore adopted the parameters for a fixed circular orbit in all cases.

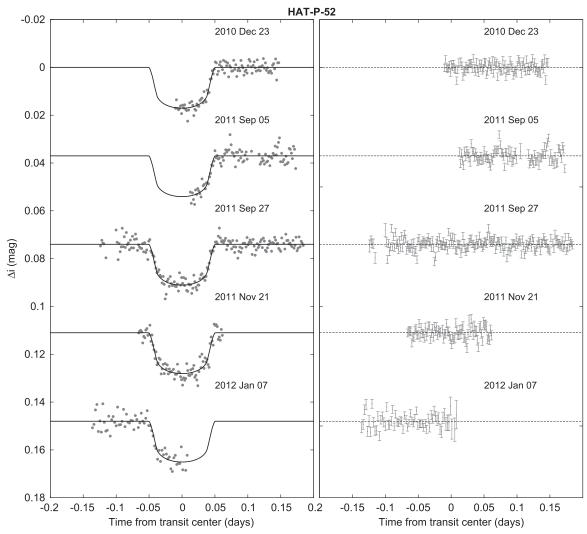


Figure 5. Similar to Figure 3; here we show the follow-up light curves for HAT-P-52. All light curves were obtained with Keplercam on the FLWO 1.2 m telescope.

3.2. Properties of the Parent Star

The stellar atmospheric parameters that we adopted for the analysis, including the effective temperature $T_{\rm eff\star}$, the surface gravity $\log g_{\star}$, the metallicity [Fe/H] and the projected equatorial rotation velocity $v \sin i$, were determined for each system using SPC. For HAT-P-50 we applied this to the TRES and FIES spectra (applying to the individual spectra and adopting the average parameter values) while for the other three systems we used the Keck/HIRES I₂-free template spectra.

We used the Yonsei-Yale (Y2; Yi et al. 2001) theoretical stellar models to determine physical parameters of the stars, such as their masses, radii, luminosities and ages, based on the measured atmospheric parameters together with the bulk stellar densities ρ_{\star} determined from our modeling of the light curves and RV measurements (Section 3.1). We generated a chain of $T_{\rm eff\star}$, [Fe/H] and ρ_{\star} values for each object, where the ρ_{\star} values are taken from the output of the DEMCMC procedure used to fit the light curves and RVs, while we assume uncorrelated Gaussian distributions for $T_{\rm eff\star}$ and [Fe/H]. For each value in the chain we interpolate the Y2 models to find a combination of M_{\star} , age and [Fe/H] which matches the three input parameters (we assume solar-scaled abundances without α -element enhancement). Combinations of $T_{\rm eff\star}$, [Fe/H] and ρ_{\star} that do

not match to a stellar model are rejected. In doing this we also reject the corresponding link in the LC+RV DEMCMC chain so that the final planetary parameters are restricted to regions of parameter space allowed by the stellar evolution models. In practice this only affects HAT-P-52 where we rejected 2.5% of the links. This is a cool star which is expected to undergo only a limited amount of stellar evolution within the age of the universe, restricting the region of $T_{\rm eff\star} + {\rm [Fe/H]} + \rho_{\star}$ parameter space which may be realized. The stellar models also provide other parameters such as R_{\star} and L_{\star} for a given M_{\star} , age and [Fe/H] combination. The result is a posterior chain of stellar parameters for each star. We use the chains to calculate the median and 68.3% confidence interval for each of the stellar parameters. These are listed in Table 3. We compare the measured $T_{\rm eff\star}$ and ρ_{\star} values for each system to the model isochrones in Figure 7.

For HAT-P-50 and HAT-P-52 we found that the median $\log g_{\star}$ values determined from this procedure differed significantly from the values estimated from the spectra. For these stars we carried out a second iteration of SPC fixing $\log g_{\star}$ to the values determined from the stellar evolution modeling. We then performed a second iteration of the LC+RV modeling, with revised limb darkening parameters, followed by a second iteration of the stellar evolution modeling. The $\log g_{\star}$ values

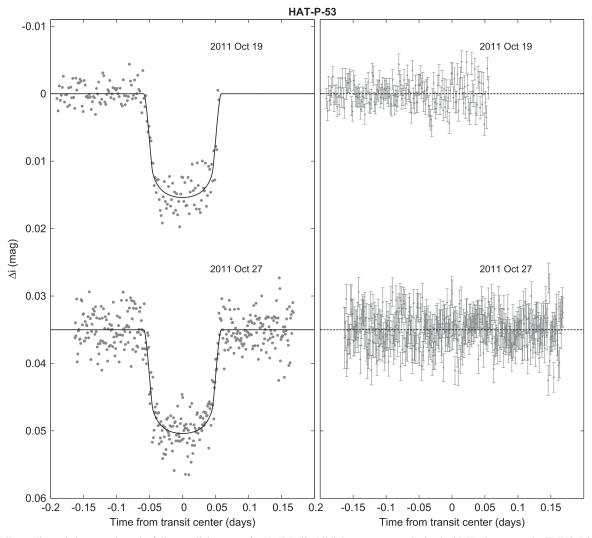


Figure 6. Similar to Figure 3; here we show the follow-up light curves for HAT-P-53. All light curves were obtained with Keplercam on the FLWO 1.2 m telescope.

had converged after this iteration. For HAT-P-51 and HAT-P-53 a second iteration of SPC was not needed.

Distances are determined for each system by comparing the measured broad-band photometry listed in Table 3 to the magnitudes predicted in each filter by the models. We allow for extinction assuming a $R_V = 3.1$ extinction law from Cardelli et al. (1989).

Based on this modeling we find that HAT-P-50 has a mass of $1.273^{+0.049}_{-0.115}\,M_{\odot}$, a radius of $1.698\pm0.071\,R_{\odot}$, an age of $3.37^{+1.44}_{-0.27}\,\rm Gyr$, and is at a distance of $497\pm21\,\rm pc$. HAT-P-51 has a mass of $0.976\pm0.028\,M_{\odot}$, a radius of $1.041^{+0.038}_{-0.022}\,R_{\odot}$, an age of $8.2\pm1.7\,\rm Gyr$, and is at a distance of $470\pm16\,\rm pc$. HAT-P-52 has a mass of $0.887\pm0.027\,M_{\odot}$, a radius of $0.893\pm0.047\,R_{\odot}$, an age of $9.4\pm4.1\,\rm Gyr$, and is at a distance of $385\pm21\,\rm pc$. Finally, HAT-P-53 has a mass of $1.093\pm0.043\,M_{\odot}$, a radius of $1.209^{+0.081}_{-0.062}\,R_{\odot}$, an age of $4.67^{+1.45}_{-0.83}\,\rm Gyr$, and is at a distance of $719\pm43\,\rm pc$.

For HAT-P-51, -52 and -53 we used the Keck/HIRES spectra to determine median $\log_{10} R'_{HK}$ activity indices. We find that all three stars are inactive in the Ca II HK region, consistent with their slow rotation and lack of photometric variability.

3.3. Excluding Blend Scenarios

In order to exclude blend scenarios we carried out an analysis following Hartman et al. (2012). We attempt to fit the available photometry (light curves, and catalog broad-band magnitudes calibrated to standard systems) for each object using a combination of three stars (two eclipsing, with a third diluting the eclipse signal) with properties taken from stellar evolution models.

For HAT-P-50, HAT-P-51 and HAT-P-53 we find that a model consisting of a planet transiting an isolated star provides a better (lower χ^2) fit to the data than any of the blend models tested. For HAT-P-50 the best-fit blend model is excluded with 1.5 σ confidence, while for both HAT-P-51 and HAT-P-53 it is excluded with 2σ confidence. We also simulated cross-correlation functions, RVs and BS measurements for the blend models tested, and found that any model that could plausibly fit the photometry for these systems (i.e., provides a fit that is no more than 5σ worse than the single star+planet model) would be easily identified as a composite stellar system based on the spectroscopy. We therefore conclude that all three of these objects are transiting planet systems.

For HAT-P-52 we similarly find that the planet+star model provides a better fit to the data than any blend model tested,

Table 3
Stellar Parameters for HAT-P-50–HAT-P-53

	HAT-P-50	HAT-P-51	HAT-P-52	HAT-P-53	
Parameter	Value	Value	Value	Value	Source
Astrometric propertie	s and cross-identifications				
2MASS-ID	07521521 + 1208218	01241564+3248387	02505320+2901206	01272906+3858053	•••
GSC-ID	GSC 0787-00340	GSC 2296-00637	GSC 1793-01136	GSC 2813-01266	•••
R.A. (J2000)	07 ^h 52 ^m 15 ^s 20	01 ^h 24 ^m 15 ^s .66	02 ^h 50 ^m 53 ^s 20	01 ^h 27 ^m 29 ^s .05	2MASS
Decl. (J2000)	+12°08′21″9	+32°48′38″8	+29°01′20″6	+38°58′05″3	2MASS
$\mu_{\mathrm{R.A.}}~(\mathrm{mas~yr^{-1}})$	10.20 ± 0.80	-9.8 ± 1.4	12.5 ± 2.1	-1.1 ± 1.8	UCAC4
$\mu_{\mathrm{Decl.}}~(\mathrm{mas~yr^{-1}})$	-4.6 ± 1.6	-16.8 ± 2.1	-24.7 ± 2.6	3.0 ± 2.2	UCAC4
Spectroscopic propert	ties				
$T_{\rm eff}_{\star}$ (K)	6280 ± 49	5449 ± 50	5131 ± 50	5956 ± 50	SPC ^b
[Fe/H]	-0.180 ± 0.080	0.270 ± 0.080	0.280 ± 0.080	0.000 ± 0.080	SPC
$v \sin i \text{ (km s}^{-1}\text{)}$	8.90 ± 0.50	1.70 ± 0.50	0.60 ± 0.50	4.10 ± 0.50	SPC
$v_{\rm mac}~({\rm km~s^{-1}})$	1.0	1.0	1.0	1.0	Assumed
$v_{\rm mic}~({\rm km~s^{-1}})$	2.0	2.0	2.0	2.0	Assumed
$\gamma_{\mathrm{RV}}~(\mathrm{km~s^{-1}})$	6.25 ± 0.10	-27.56 ± 0.10	61.50 ± 0.10	-16.99 ± 0.10	TRES
$\log_{10} R'_{\rm HK}^{\rm c}$		-5.057 ± 0.050	-5.154 ± 0.089	-4.919 ± 0.042	HIRES
Photometric propertie	es				
B (mag)	12.282 ± 0.050	14.261 ± 0.070	15.183 ± 0.050		APASS,TASS ^d
V (mag)	11.762 ± 0.030	13.440 ± 0.040	14.068 ± 0.020	13.73 ± 0.18	APASS,TASS ^d
I_C (mag)	11.194 ± 0.052	12.67 ± 0.12	13.02 ± 0.17	13.13 ± 0.12	TASS
g (mag)	11.973 ± 0.050	13.839 ± 0.050	14.631 ± 0.060		APASS
r (mag)	11.650 ± 0.030	13.194 ± 0.030	13.677 ± 0.080		APASS
i (mag)	11.550 ± 0.020	12.998 ± 0.040	13.441 ± 0.090		APASS
J (mag)	10.816 ± 0.021	12.039 ± 0.022	12.195 ± 0.022	12.468 ± 0.023	2MASS
H (mag)	10.545 ± 0.020	11.645 ± 0.023	11.745 ± 0.022	12.202 ± 0.026	2MASS
K_s (mag)	10.500 ± 0.018	11.614 ± 0.020	11.621 ± 0.021	12.100 ± 0.019	2MASS
Derived properties					
$M_{\star}~(M_{\odot})$	$1.273^{+0.049}_{-0.115}$	0.976 ± 0.028	0.887 ± 0.027	1.093 ± 0.043	$YY+a/R_{\star}+SPC^{\circ}$
$R_{\star} \ (R_{\odot})$	1.698 ± 0.071	$1.041^{+0.038}_{-0.029}$	0.893 ± 0.047	$1.209^{+0.081}_{-0.062}$	$YY+a/R_{\star}+SPC$
$\log g_{\star} (\text{cgs})$	4.072 ± 0.029	4.392 ± 0.027	4.483 ± 0.051	4.310 ± 0.043	$YY+a/R_{\star}+SPC$
$\rho_{\star} \text{ (g cm}^{-3})$	0.357 ± 0.037	$1.223^{+0.100}_{-0.135}$	1.75 ± 0.29	0.87 ± 0.13	$YY+a/R_{\star}+SPC$
L_{\star} (L_{\odot})	4.01 ± 0.38	0.859 ± 0.070	0.496 ± 0.060	$1.65^{+0.24}_{-0.18}$	$YY+a/R_{\star}+SPC$
M_V (mag)	3.27 ± 0.11	5.055 ± 0.095	5.73 ± 0.13	4.27 ± 0.13	$YY+a/R_{\star}+SPC$
M_K (mag,ESO)	2.052 ± 0.093	3.268 ± 0.071	3.69 ± 0.12	2.83 ± 0.12	$YY + a/R_{\star} + SPC$
Age (Gyr)	$3.37^{+1.44}_{-0.27}$	8.2 ± 1.7	9.4 ± 4.1	$4.67^{+1.45}_{-0.83}$	$YY + a/R_{\star} + SPC$
A_V (mag)	$0.011^{+0.056}_{-0.011}$	$0.012^{+0.071}_{-0.012}$	0.412 ± 0.052	0.21 ± 0.14	$YY + a/R_{\star} + SPC$
Distance (pc)	497 ± 21	470 ± 16	385 ± 21	719 ± 43	$YY + a/R_{\star} + SPC$
Distance (pc)	T) /	470 ± 10	303 ± 21	/1/ ± 7 3	1 1 \(\pi\at\)/ N\(\pi\) \(\pi\) (

however the best-fit blend model differs by only 0.5σ from the planet+star model. We also find that there is a range of models consisting of a blend between a bright foreground star, and a background stellar eclipsing binary that is between 0.35 and 4 mag further in distance modulus than the foreground star, which cannot be ruled out based on the photometry or BS spans. For these models the simulated BS variations have a scatter that is below the 43 m s⁻¹ scatter in the Keck/HIRES data, if we allow for a difference in the γ velocities of the foreground star and background binary. We find, however, that similar to the case of HAT-P-49 (Bieryla et al. 2014), the

expected form of the RV variations in these blends is significantly different from the observed sinusoidal variation, even though the overall amplitude of the variations is comparable (Figure 8). We conclude that although the photometry and BS measurements for HAT-P-52 can be fit by a blended stellar eclipsing binary model, the RV observations cannot be.

While we can rule out the possibility that any of these objects is a blended stellar eclipsing binary system, we cannot rule out the possibility that one or more of these transiting planet systems also has a stellar companion. For HAT-P-50, we

^a We show the median value and 68.3% confidence interval for each parameter. If the upper and lower confidence bounds are equal in absolute value to within a factor of 1.3, then we display symmetric uncertainties, otherwise asymmetric uncertainties are displayed. Parameters are displayed to two significant digits in their uncertainties.

^b SPC—"Stellar Parameter Classification" routine for the analysis of high-resolution spectra (Buchhave et al. 2012), applied to the TRES and FIES spectra of HAT-P-50, and to the Keck/HIRES I₂-free template spectra of HAT-P-51, HAT-P-52 and HAT-P-53. These parameters rely primarily on SPC, but have a small dependence also on the iterative analysis incorporating the isochrone search and global modeling of the data, as described in the text.

^c The median of the $\log_{10} R'_{HK}$ values measured from the individual Keck/HIRES spectra for each target. The uncertainty is the standard error on the median.

d From APASS DR6 for HAT-P-50, HAT-P-51 and HAT-P-52 as listed in the UCAC 4 catalog (Zacharias et al. 2012). From TASS Mark IV (Droege et al. 2006) for HAT-P-53.

^e YY+ a/R_{\star} +SPC—Based on the YY isochrones (Yi et al. 2001), a/R_{\star} as a luminosity indicator, and the SPC results.

 ${\bf Table~4} \\ {\bf Relative~Radial~Velocities,~Bisector~Spans,~and~Activity~Index~Measurements~for~HAT-P-50-HAT-P-53} \\$

BJD	RV ^a	$\sigma_{ m RV}^{^{b}}$	BS	$\sigma_{ m BS}$	S ^c	Phase	Instrumen
(2,454,000+)	$(m s^{-1})$	$(m s^{-1})$	$(m s^{-1})$	$(m s^{-1})$			
			HAT-P-	50			
1903.95158	169.24	31.82				0.656	TRES
1911.98432	-149.26	31.82		•••	•••	0.229	TRES
1941.89144	-5.12	65.07				0.808	TRES
1957.72714	81.84	63.24				0.881	TRES
1958.68285	-19.27	59.81				0.187	TRES
1960.70621	-26.06	73.39				0.835	TRES
1964.90560	-161.79	16.35	-44.94	22.34		0.180	HDS
1964.91336	-158.48	15.07	-40.90	21.84		0.182	HDS
1964.92112	-164.86	14.23	-54.18	20.02		0.185	HDS
1964.93269			-62.87	21.17		0.189	HDS
1964.94740	•••	•••	-62.65	21.82	•••	0.193	HDS
1964.96211	•••	•••	-61.14	22.32		0.198	HDS
1965.06347	-184.08	15.46	-110.01	24.62	•••	0.231	HDS
1965.07123	-196.36	14.93	-153.60	27.34		0.233	HDS
1966.86139	143.00	14.72	-32.02	20.00		0.807	HDS
1966.87609	137.51	13.33	-19.54	19.70		0.811	HDS
1967.86542	-96.04	21.28	-7.35	21.69		0.128	HDS
1967.87318	-93.64	18.64	-15.27	20.80	•••	0.131	HDS
1967.88093	-87.90	16.20	0.26	18.99		0.133	HDS
1967.88867	-108.44	17.37	-9.93	20.59	•••	0.135	HDS
2000.39479	78.60	23.25		•••	•••	0.547	FIES
2001.40519	121.33	23.25		•••	•••	0.871	FIES
2002.47018	-191.77	30.26		•••	•••	0.212	FIES
2003.40044	4.13	54.05		•••	•••	0.510	FIES
2004.38851	120.16	31.15				0.827	FIES
2191.13792	121.23	22.53	45.30	19.61	•••	0.644	HDS
2191.14223	129.48	26.61	129.85	21.78		0.645	HDS
2191.14652	184.86	29.91	496.30	30.08		0.647	HDS
2192.12442	48.71	17.29	7.33	16.97	•••	0.960	HDS
2192.12871	45.28	23.29	-3.33	20.31		0.961	HDS
2192.13300	28.57	21.63	9.00	17.56		0.963	HDS
2193.11572	-151.84	16.13	-7.12	19.16	•••	0.277	HDS
2193.12002	-121.63	23.24	-5.25	17.21	•••	0.279	HDS
2193.12433	-127.80	20.99	2.08	16.32	•••	0.280	HDS
		1	HAT-P-	 51		ı	
1052 00027	42.75	2.52			0.1550	0.217	HIDEG
1853.80027	-42.75	2.53	-16.75	5.54	0.1550	0.317	HIRES
1853.81798	•••	•••	-2.36	6.06	0.1300	0.322	HIRES
1879.85898		2.69	10.56	6.81	0.1630	0.495	HIRES
1879.87608	7.25	2.68	8.32	6.08	0.1570	0.499	HIRES
1880.97599	42.01	2.48	9.54	5.32	0.0769	0.760	HIRES
1903.95906	-35.87	2.63	-42.11	21.39	0.1550	0.209	HIRES
1944.73569	24.93	2.55	-9.88 5.14	7.15	0.1170	0.876	HIRES
1960.81411	31.81	3.23	5.14	7.02	0.1600	0.688	HIRES
1964.71582	44.69	13.17	-0.33	26.24	•••	0.613	HDS
1964.72359	27.51	11.37	-23.77	23.80	•••	0.615	HDS
1964.73475	21.63	11.55	7.03	29.96	•••	0.617	HDS
1964.74946	25.14	9.83	3.26	34.15	•••	0.621	HDS
1964.76417	33.95	9.59	0.65	35.27	•••	0.624	HDS
1965.71533	32.14	15.07	-2.89	24.12	•••	0.850	HDS
1965.73005	29.21	12.47	9.32	36.71	•••	0.853	HDS
1965.74477	33.24	11.95	-14.30	27.64	•••	0.857	HDS
1965.75948	34.67	14.11	-16.82	27.55	•••	0.860	HDS
1965.77418	13.59	12.75	21.67	22.10	•••	0.864	HDS
1965.78890	15.87	21.41	23.88	25.83	•••	0.866	HDS
1966.72018	•••	•••	-4.21	31.52	•••	0.088	HDS
1966.73489	•••	•••	9.59	32.96	•••	0.092	HDS
1966.74959	•••	•••	4.25	32.50	•••	0.095	HDS
1966.76429	•••	•••	5.05	34.50	•••	0.099	HDS
1966.77907	-12.89	12.16	-0.33	34.37	•••	0.102	HDS
	22.00	11.65	27.17	29.63		0.106	HDS
1966.79377 1966.80848	-33.08 -13.58	15.24	5.11	13.87		0.109	HDS

Table 4 (Continued)

			(Continue	(34)			
BJD (2,454,000+)	$RV^a \ (m\ s^{-1})$	$\sigma_{\rm RV}^{}$ (m s ⁻¹)	BS (m s ⁻¹)	$\sigma_{\rm BS}$ (m s ⁻¹)	S ^c	Phase	Instrument
1967.72003	-24.46	14.33	-2.79	22.98		0.325	HDS
1967.73475	-48.37	13.90	-12.59	23.40		0.329	HDS
1967.74946	-42.32	13.39	-11.16	21.89		0.332	HDS
1967.76417	-34.03	12.75	0.39	20.57		0.336	HDS
1967.77888	-28.16	13.62	3.97	17.43		0.339	HDS
1967.79359	-28.23	14.33	-32.17	31.51		0.343	HDS
			HAT-P-5	52	,	,	,
1611.81789	134.02	4.23	17.97	81.51	0.2500	0.738	HIRES
1853.86184	90.96	3.67	-6.05	13.12	0.1870	0.639	HIRES
1853.88098	•••		67.06	32.55	0.1230	0.646	HIRES
1879.90065	-62.91	4.21	-11.44	32.23	0.1220	0.095	HIRES
1880.99970	1.46	3.24	10.18	16.84	0.1500	0.494	HIRES
1882.08871	76.62	7.72	-77.06	46.76	0.4450	0.890	HIRES
1972.84557	102.30	4.25				0.849	HIRES
2139.06062	-134.45	3.86	-0.66	15.61	0.1360	0.212	HIRES
		,	HAT-P-5	53	,		,
1877.91488	217.41	4.13	3.37	8.66	0.1820	0.708	HIRES
1879.81971	220.06	3.91	-8.64	5.38	0.1710	0.679	HIRES
1879.83898	•••	•••	-6.30	5.05	0.1700	0.689	HIRES
1880.95723	-228.59	3.82	4.64	4.22	0.1740	0.259	HIRES
1944.84748	187.44	5.04	11.55	4.67	0.1010	0.829	HIRES
1960.79667	43.84	4.68	-10.07	13.55	0.1430	0.959	HIRES
1972.75173	-68.38	4.23	-14.42	7.85	0.1570	0.054	HIRES

Notes. Note that for the iodine-free template exposures we do not measure the RV but do measure the BS and S index. Such template exposures can be distinguished by the missing RV value.

Table 5
Light Curve Data for HAT-P-50–HAT-P-53

Object ^a	BJD ^b	Mag ^c	$\sigma_{ m Mag}$	Mag(orig) ^d	Filter	Instrument
	(2,400,000+)					
HAT-P-50	54863.83699	0.00928	0.00393		r	HATNet
HAT-P-50	54935.64419	-0.00034	0.00517		r	HATNet
HAT-P-50	54838.86248	0.00069	0.00443		r	HATNet
HAT-P-50	54888.81494	-0.00915	0.00442		r	HATNet
HAT-P-50	54792.03291	0.00668	0.00450		r	HATNet
HAT-P-50	54910.67022	0.00400	0.00418		r	HATNet
HAT-P-50	54863.84110	0.00001	0.00388		r	HATNet
HAT-P-50	54935.64826	0.00737	0.00652		r	HATNet
HAT-P-50	54838.86690	0.00070	0.00433		r	HATNet
HAT-P-50	54888.81903	0.00426	0.00441		r	HATNet

Notes

(This table is available in its entirety in machine-readable and Virtual Observatory (VO) forms.)

find that models including a faint companion with $M>0.6\,M_\odot$ provide a slightly worse fit to the data than models without a companion. The difference in χ^2 is small, however, and we can

only rule out a stellar companion with $M>1.2\,M_\odot$ at greater than 3σ confidence. For HAT-P-51, models with a companion having $M>0.5\,M_\odot$ have a slightly worse fit to the data, but we

^a The zero-point of these velocities is arbitrary. An overall offset γ_{rel} fitted to these velocities in Section 3.1 has *not* been subtracted.

b Internal errors excluding the component of astrophysical jitter considered in Section 3.1.

^c Chromospheric activity index calculated following Isaacson & Fischer (2010).

^a Either HAT-P-50, HAT-P-51, HAT-P-52, or HAT-P-53.

b Barycentric Julian Date is computed directly from the UTC time without correction for leap seconds.

^c The out-of-transit level has been subtracted. These magnitudes have been subjected to the EPD and TFA procedures, carried out simultaneously with the transit fit. ^d Raw magnitude values without application of the EPD and TFA procedures. These are provided only for the follow-up observations. For HATNet, the transits are only detectable after applying the noise filtering methods.

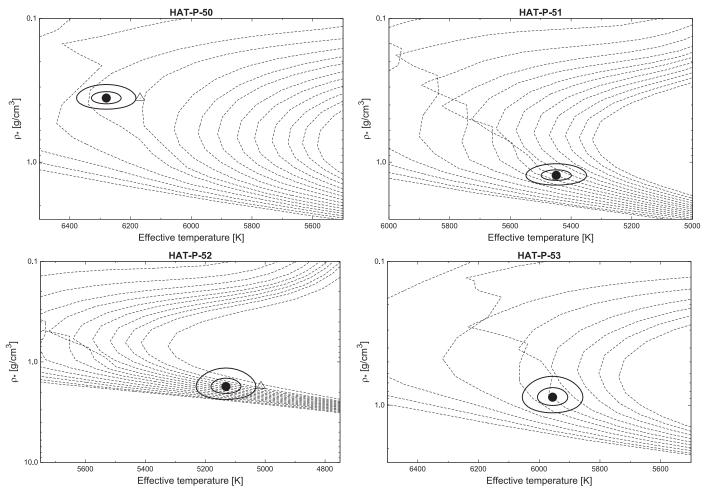


Figure 7. Model isochrones from Yi et al. (2001) for the measured metallicities of HAT-P-50 (upper left), HAT-P-51 (upper right), HAT-P-52 (lower left) and HAT-P-53 (lower right). In each case we show models for several different ages, with younger models being on the left and older ones on the right. For HAT-P-50 and HAT-P-51 and HAT-P-52 we show ages of 0.2 Gyr and 1.0–14.0 Gyr in 1.0 Gyr increments. For HAT-P-53 we show ages of 0.2 Gyr and 1.0–9.0 Gyr in 1.0 Gyr increments. The adopted values of $T_{\text{eff}\star}$ and ρ_{\star} are shown together with their 1σ and 2σ confidence ellipsoids. The initial values of $T_{\text{eff}\star}$ and ρ_{\star} from the first SPC and light curve analyses are represented with a triangle for HAT-P-50 and HAT-P-52. Note the logarithmic vertical axes, and the different scales used in each panel.

can only rule out companions with $M>0.95~M_{\odot}$ at greater than 3σ confidence. For HAT-P-52, companions with $M>0.35~M_{\odot}$ provide a slightly worse fit to the data, but all companions up to the mass of HAT-P-52 are permitted to within 3σ . For HAT-P-53 companions with $M>0.7~M_{\odot}$ provide a slightly worse fit, but all companions up to the mass of HAT-P-52 are permitted to within 3σ .

4. DISCUSSION

In this paper we presented the discovery and characterization of four TEPs from the HATNet survey, including three hot Jupiters (HAT-P-50b, HAT-P-52b and HAT-P-53b) and a hot Saturn (HAT-P-51b). All four planets have masses and radii determined to better than 10% precision. The mass uncertainties are 5.4%, 5.8%, 3.5%, and 3.8% for HAT-P-50b through HAT-P-53b, respectively, while the respective radius uncertainties are 5.0%, 4.2%, 7.1%, and 6.9%. The stars HAT-P-50, -51, and -53 also have fairly precise isochrone-based age determinations (uncertainty less than 2 Gyr) thanks to their favorable position within the $T_{\rm eff}$ - ρ_{\star} plane (Figure 7).

In Figure 9 we show the location of these planets on a mass-radius diagram, comparing them to the full sample of confirmed TEPs with $0.1 < M_p < 10 \, M_J$. The new planets all

fall within the range of values already seen by other planets, with HAT-P-51b falling near the upper envelope of the distribution of points in the mass-radius diagram, and HAT-P-52b falling near the lower envelope. We also show the location of each planet on a $T_{\rm eq}$ -radius diagram. Again we find that the planets all follow the well-established trends. While not atypical compared to other known exoplanets, these objects contribute to the growing sample of well-characterized planets which may be used to explore the population of planets in the Galaxy through statistical methods.

In terms of potential for additional follow-up observations, we conclude that it should be feasible to measure the Rossiter-McLaughlin effect for HAT-P-50b, HAT-P-51b and HAT-P-53b using Subaru/HDS or Keck/HIRES. For HAT-P-50b the expected amplitude of the R-M effect is 42 m s⁻¹ for an aligned orbit (using Equation (40) in Winn 2010). For HAT-P-51b the expected amplitude is 27 m s⁻¹, and for HAT-P-53b it is 48 m s⁻¹. The Subaru/HDS velocity residuals for HAT-P-50 have an rms of 23 m s⁻¹, with a median exposure time of 10 minutes. Assuming 20 such exposures are obtained over the course of a single transit, it should be possible to measure the R-M amplitude to a precision of 5σ (based on fitting models to simulated observations). For HAT-P-51, the Keck/HIRES RVs have a residual rms of 5.4 m s⁻¹, and a median exposure time

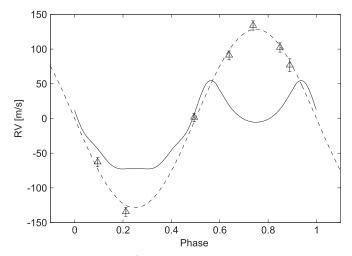


Figure 8. Phase-folded Keck/HIRES RVs for HAT-P-52 compared to the best-fit planetary orbit (dashed curve) and the best-fit RVs from a blended stellar eclipsing binary model (solid curve). This same blend model has BS variations that are below the observed scatter, and fits the photometric data, however it does not reproduce the form of the RV variation, which is well described by a transiting planet. The blend-model fit shown here consists of a 0.88 M_{\odot} foreground star blended with a 0.84 M_{\odot} +0.13 M_{\odot} eclipsing binary that has a distance modulus 0.35 mag greater than the foreground star, and which has a γ velocity that is 70 km s⁻¹ different from that of the foreground star. Reducing the difference in γ velocities creates a more symmetric RV variation, but also results in the RV variation going to 0 m s⁻¹ at both phases 0.25 and 0.75. All other blend models simulated have RV variations that provide even poorer fits to the observations.

of 25 minutes. Seven of these exposures could be collected over a single transit, allowing a 9σ detection of the R-M amplitude. For HAT-P-53, the Keck/HIRES RVs have a residual of 11 m s $^{-1}$ and an exposure time of 25 minutes. For this system it should be possible to collect 6 similar exposures during a transit, and measure the R-M amplitude with 8σ confidence. For HAT-P-52b the R-M amplitude is only $\lesssim\!\!7$ m s $^{-1}$ (limited by the very slow rotation), and we would not expect to detect it in a single transit with better than 2σ confidence.

The conclusion that the R-M effect should be easier to detect for both HAT-P-51 and HAT-P-53 than for HAT-P-50, despite both stars being significantly fainter than HAT-P-50, and despite both stars having a lower $v \sin i$, may be counter intuitive. The RV observations for HAT-P-51 and HAT-P-53 are both significantly higher precision than those for HAT-P-50, even though the HAT-P-50 observations have higher S/N. Some of the difference may be due to the different instruments (Subaru/HDS for HAT-P-50 versus Keck/HIRES for HAT-P-51 and HAT-P-53). However, slower rotation and cooler surface temperatures are also factors which tend to improve the RV precision. In this respect we expect HAT-P-51 to have higher precision than HAT-P-53 at fixed S/N, and HAT-P-53 to have higher precision than HAT-P-50 at fixed S/N, which is what we see.

Measuring the R-M effect for HAT-P-51b may be of particular interest due to its small mass. HAT-P-11b and Kepler-63b are the only planets smaller than HAT-P-51b for which this effect has been measured to date (Winn et al. 2010 and Sanchis-Ojeda et al. 2013; the obliquity has also been measured for the Kepler-30 system by star-spot crossings, see Sanchis-Ojeda et al. 2012).

While the R-M effect should be detectable for HAT-P-50b, HAT-P-51b and HAT-P-53b, due to the relatively small value of R_p/R_{\star} for HAT-P-50b, and the faintness of the other targets, none of the new planets are particularly well-suited for atmospheric characterization.

HATNet operations have been funded by NASA grants NNG04GN74G, NNX08AF23G, and NNX13AJ15G. Follow-up of HATNet targets has been partially supported through NSF grant AST-1108686. G. Á. B, Z. C. and K. P. acknowledge partial support from NASA grant NNX09AB29G. J. H. acknowledges support from NASA grant NNX14AF87G. K. P. acknowledges support from NASA grant NNX13AQ62G. G. T. acknowledges partial support from NASA grant NNX14AB83G. We acknowledge partial support also from the Kepler Mission under NASA Cooperative Agreement NCC2-1390 (D.W.L., PI). Data presented in this paper are based on observations obtained at

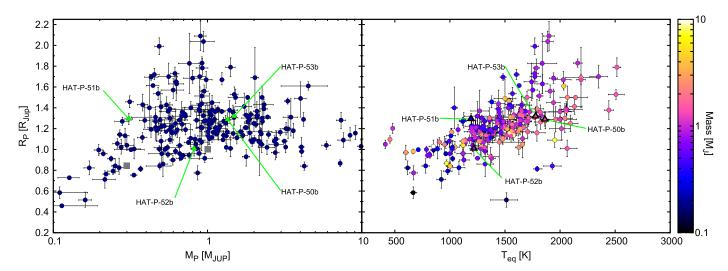


Figure 9. Left: mass–radius diagram for transiting planets with $0.1\,M_{\rm J} < M < 10\,M_{\rm J}$. The four planets discovered here are indicated. The two filled gray squares show Saturn and Jupiter. The parameters for other transiting planets are compiled from the literature (c.f. http://www.exoplanets.org accessed 2015 March 3). Right: planet radius vs. estimated equilibrium temperature (assuming zero albedo and complete redistribution of heat) for the same sample of planets as shown at left. Symbols are assigned colors based on the planetary masses.

Table 6 Orbital and Planetary Parameters for HAT-P-50b-HAT-P-53ba

	HAT-P-50b	HAT-P-51b	HAT-P-52b	HAT-P-53b
Parameter	Value	Value	Value	Value
Light curve parameters				
P (days)	3.1220109 ± 0.0000065	4.2180278 ± 0.0000059	2.7535953 ± 0.0000094	1.9616241 ± 0.0000039
$T_c \text{ (BJD)}^{\mathbf{b}}$	2456285.90993 ± 0.00036	$2456194.12204 \pm 0.00040$	$2455852.10326 \pm 0.00041$	2455829.44781 ± 0.00044
$T_{14} (\mathrm{days})^{\mathrm{b}}$	0.1531 ± 0.0011	0.1403 ± 0.0016	0.1003 ± 0.0017	0.1164 ± 0.0017
$T_{12} = T_{34} \text{ (days)}^{b}$	0.0176 ± 0.0013	0.0170 ± 0.0012	0.0130 ± 0.0018	0.0135 ± 0.0016
a/R_{\star}	5.68 ± 0.19	$10.48^{+0.28}_{-0.40}$	8.89 ± 0.49	5.61 ± 0.28
$\zeta/R_{\star}^{\ c}$	14.710 ± 0.077	16.21 ± 0.12	22.88 ± 0.27	19.42 ± 0.17
R_p/R_\star	0.0782 ± 0.0012	0.1278 ± 0.0020	0.1161 ± 0.0027	0.1120 ± 0.0019
b^2	$0.395^{+0.041}_{-0.050}$	$0.077^{+0.055}_{-0.052}$	$0.213^{+0.096}_{-0.098}$	$0.142^{+0.099}_{-0.090}$
$b \equiv a \cos i/R_{\star}$	$0.629^{+0.032}_{-0.041}$	$0.277^{+0.085}_{-0.119}$	$0.461^{+0.094}_{-0.122}$	$0.38^{+0.11}_{-0.15}$
i (deg)	83.65 ± 0.57	88.48 ± 0.57	87.02 ± 0.86	86.2 ± 1.5
Limb-darkening coefficients ^d				
c_1 , i (linear term)	0.1965	0.3348	0.3908	0.2387
c_2 , i (quadratic term)	0.3570	0.2989	0.2628	0.3447
RV parameters				
$K \text{ (m s}^{-1})$	161.3 ± 5.6	39.5 ± 2.2	128.4 ± 3.8	226.8 ± 6.0
e^{e}	< 0.115	< 0.123	< 0.047	< 0.134
RV jitter HIRES (m s ⁻¹) ^f		4.3 ± 1.2	5.2 ± 1.9	9.3 ± 3.2
RV jitter HDS (m s ⁻¹)	0.7 ± 7.1	0.0 ± 1.4		•••
RV jitter TRES (m s ⁻¹)	68 ± 38			•••
RV jitter FIES (m s ⁻¹)	0.00 ± 0.91			
Secondary eclipse parameters				
T_s (BJD)	$2456287.47093 \pm 0.00036$	$2456196.23106 \pm 0.00040$	$2455853.48006 \pm 0.00041$	$2455830.42863 \pm 0.00044$
$T_{s,14}$ (days)	0.1531 ± 0.0011	0.1403 ± 0.0016	0.1003 ± 0.0017	0.1164 ± 0.0017
$T_{s,12}$ (days)	0.0176 ± 0.0013	0.0170 ± 0.0012	0.0130 ± 0.0018	0.0135 ± 0.0016
Planetary parameters				
$M_p (M_{\rm J})$	1.350 ± 0.073	0.309 ± 0.018	0.818 ± 0.029	1.484 ± 0.056
$R_p(R_{\rm J})$	1.288 ± 0.064	1.293 ± 0.054	1.009 ± 0.072	1.318 ± 0.091
$C(M_p, R_p)^{\mathbf{g}}$	0.48	-0.03	-0.15	0.34
$\rho_p \ (\mathrm{g \ cm^{-3}})$	0.78 ± 0.11	0.178 ± 0.024	0.98 ± 0.21	0.80 ± 0.15
$\log g_p \text{ (cgs)}$	3.302 ± 0.038	$2.661^{+0.037}_{-0.051}$	3.296 ± 0.065	3.325 ± 0.055
a (AU)	$0.04530^{+0.00058}_{-0.00140}$	0.05069 ± 0.00049	0.03694 ± 0.00038	0.03159 ± 0.00042
$T_{\rm eq}$ (K)	1862 ± 34	1192 ± 21	1218 ± 37	1778 ± 48
$\Theta^{\mathbf{h}}$	0.0751 ± 0.0044	0.0247 ± 0.0018	0.0673 ± 0.0050	0.0649 ± 0.0046
$\log_{10}\langle F\rangle(\text{cgs})^{i}$	9.433 ± 0.032	8.659 ± 0.031	8.696 ± 0.052	9.354 ± 0.046

the HAT station at the Submillimeter Array of SAO, and the HAT station at the Fred Lawrence Whipple Observatory of SAO. The authors wish to acknowledge the very significant cultural role and reverence that the summit of Mauna Kea has always had within the indigenous Hawaiian community. We are most fortunate to have the opportunity to conduct observations from this mountain. This research has made use of Keck telescope time granted through NOAO (program A245Hr) and NASA (N154Hr,

^a We show the median value and 68.3% confidence interval for each parameter. If the upper and lower confidence bounds are equal in absolute value to within a factor of 1.3, then we display symmetric uncertainties, otherwise asymmetric uncertainties are displayed. For the b^2 and b parameters, which have strict lower bounds, we only show asymmetric uncertainties. Parameters are displayed to two significant digits in their uncertainties.

b Times are in Barycentric Julian Date calculated directly from UTC without correction for leap seconds. Tc: Reference epoch of mid transit that minimizes the correlation with the orbital period. T_{14} : total transit duration, time between first to last contact; $T_{12} = T_{34}$: ingress/egress time, time between first and second, or third and fourth contact.

^c Reciprocal of the half duration of the transit used as a jump parameter in our DEMCMC analysis in place of a/R_{\star} . It is related to a/R_{\star} by the expression $\zeta/R_\star = a/R_\star (2\pi (1+e\sin\omega))/(P\sqrt{1-b^2}\sqrt{1-e^2})$ (Bakos et al. 2010). d Values for a quadratic law, adopted from the tabulations by Claret (2004) according to the spectroscopic (SPC) parameters listed in Table 3.

e As discussed in Section 3.1 the adopted parameters for all four systems are determined assuming circular orbits. We also list the 95% confidence upper limit on the eccentricity determined when $\sqrt{e} \cos \omega$ and $\sqrt{e} \sin \omega$ are allowed to vary in the fit.

Term added in quadrature to the formal RV uncertainties for each instrument. This is treated as a free parameter in the fitting routine, and as a result has an uncertainty. For HIRES we include an empirical prior constraint following Hartman et al. (2014).

^g Correlation coefficient between the planetary mass M_p and radius R_p .

^h The Safronov number is given by $\Theta = \frac{1}{2}(V_{\rm esc}/V_{\rm orb})^2 = (a/R_p)(M_p/M_{\star})$ (see Hansen & Barman 2007).

¹ Incoming flux per unit surface area, averaged over the orbit.

N130Hr). This research was made possible through the use of the AAVSO Photometric All-Sky Survey (APASS), funded by the Robert Martin Ayers Sciences Fund.

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